

# WINPOWER Project (Feb. 2011 – Feb. 2015) - 11 partners



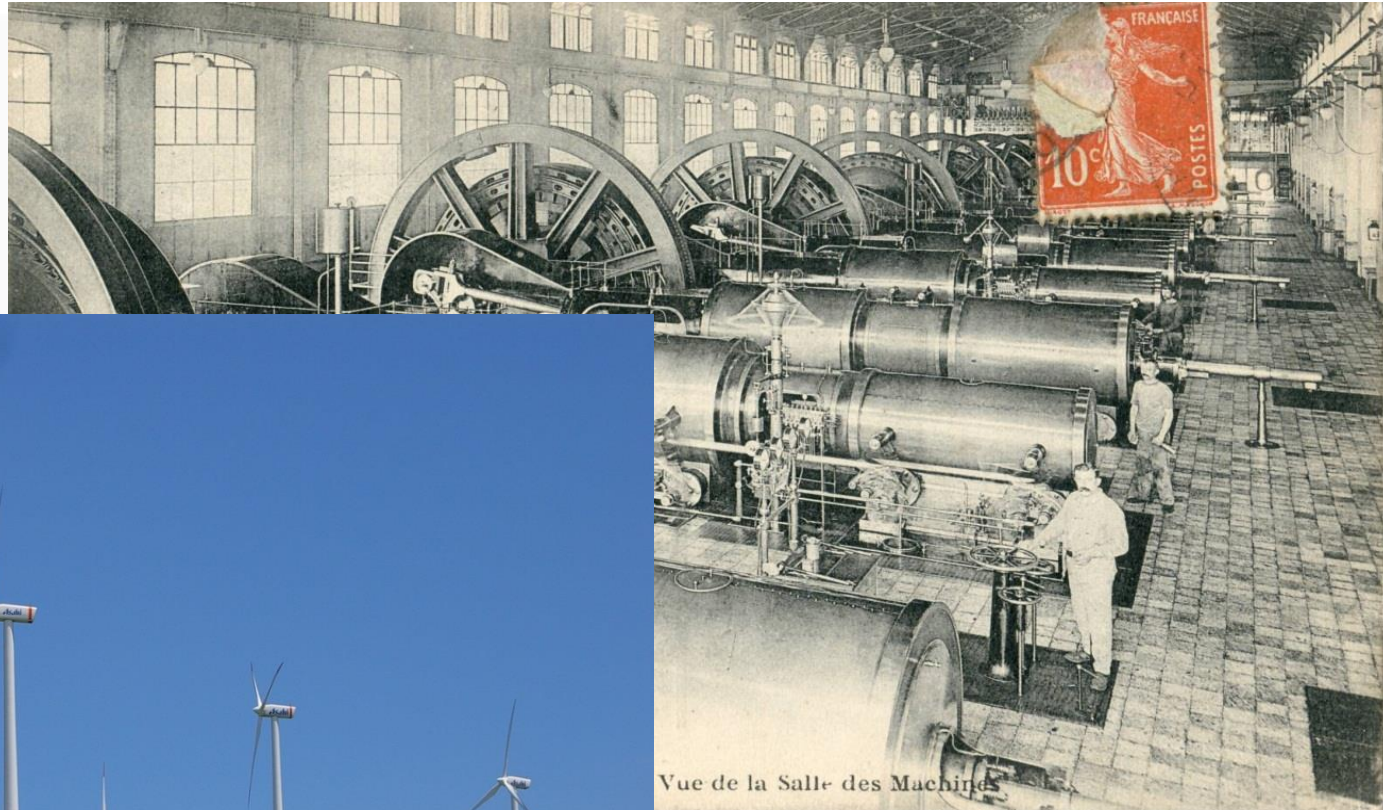
ANR-10-SEGI-016



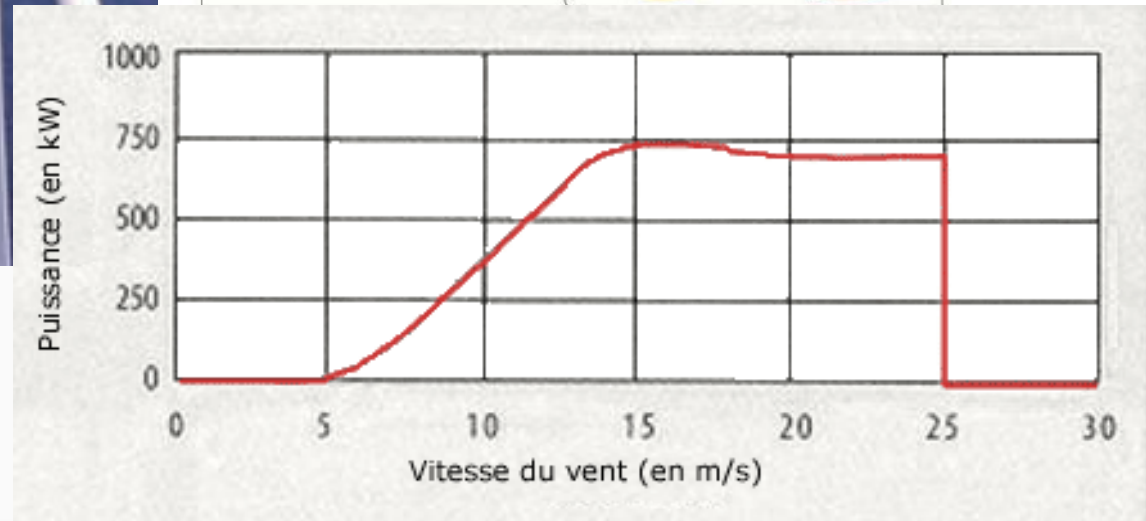
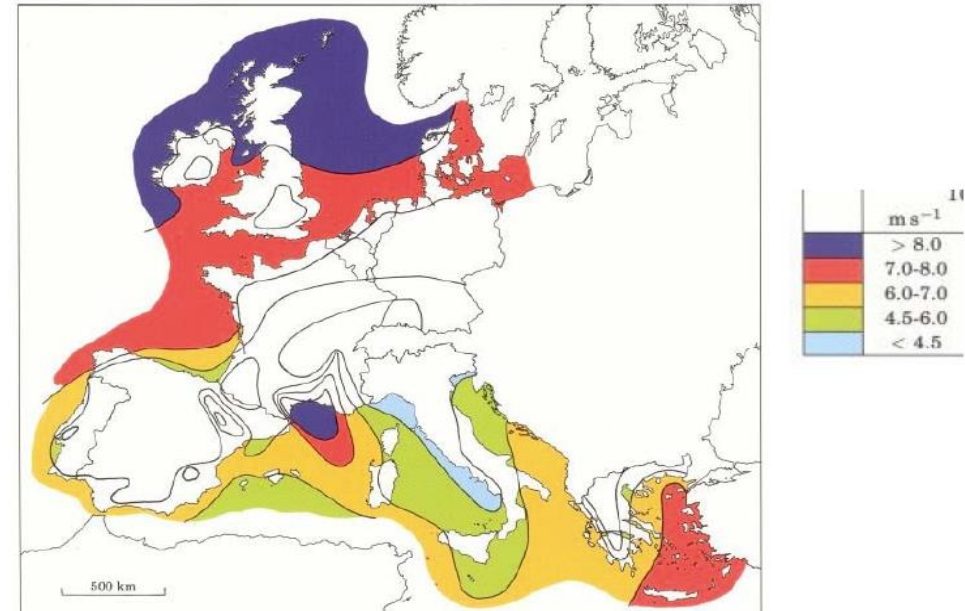
**Coordinator: Gilney Damm**  
**EECI / Evry Val d'Essonne University**

# *Motivation*

# *Power networks are changing...*

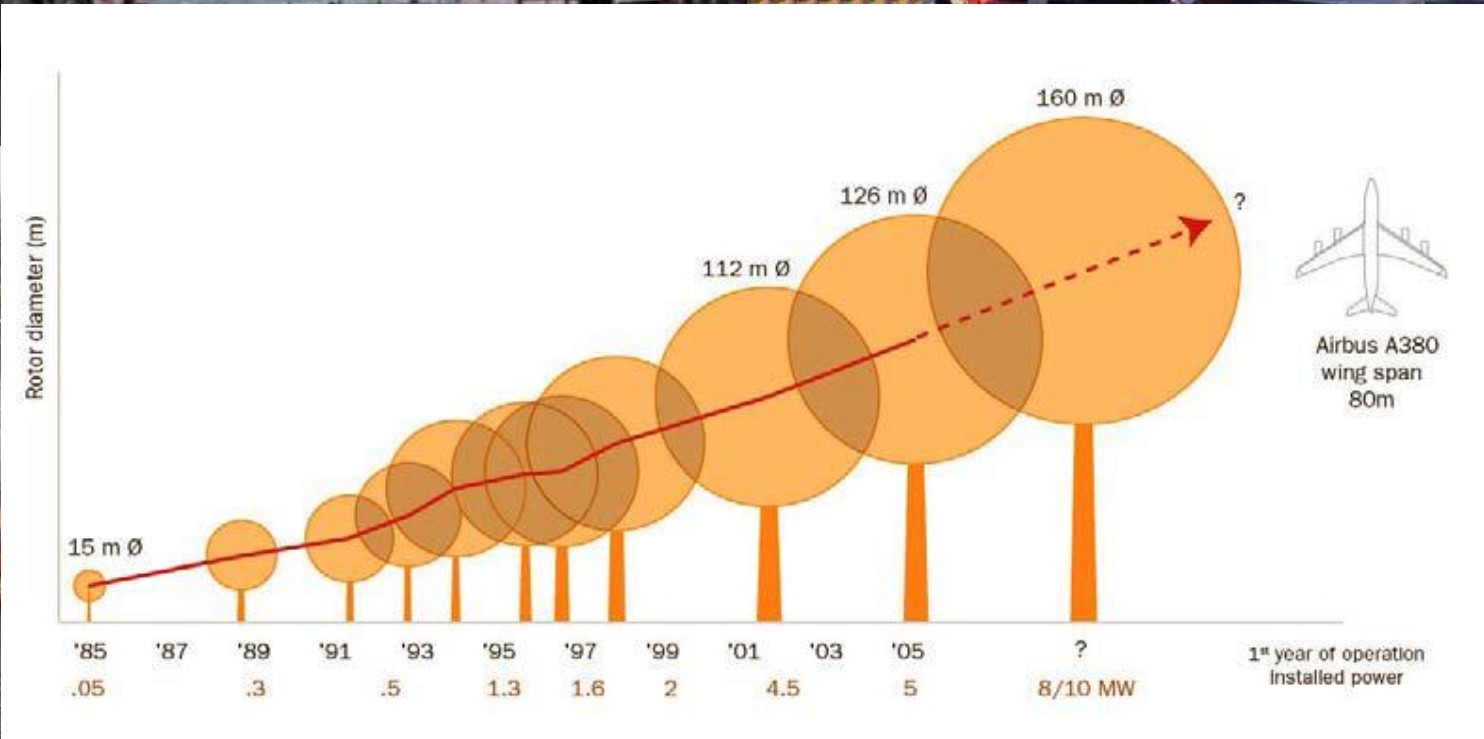


# Off-shore Wind power generation



Stronger, steadier and more predictable

# Ever growing Off-shore Wind Farms



# Marine current / Tidal Power

EDF - Paimpol Brehat (Brittany - France)



Siemens SeaGen - Strangford Lough  
in Northern Ireland

# *Solar Power – Solar Thermodynamic*

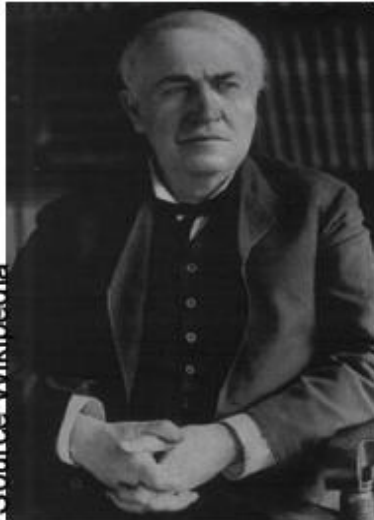


*Large scale integration  
of renewables –  
particularly off-shore*



# *New (?) possibilities – HVDC*

**Thomas Alva Edison  
(1847–1931)**



Source: Wikipedia

**Nikola Tesla  
(1856–1943)**



Source: Wikipedia

## **The War of Currents**

**Edison and Tesla Fight Over How  
To Power the World**

***DC or AC ?***

**George Westinghouse  
(1846–1914)**



Source: Wikipedia

UNITED STATES PATENT OFFICE.

GEORGE WESTINGHOUSE, JR., OF PITTSBURG, PENNSYLVANIA.

SYSTEM OF ELECTRICAL DISTRIBUTION.

SPECIFICATION forming part of Letters Patent No. 373,035, dated November 8, 1887.

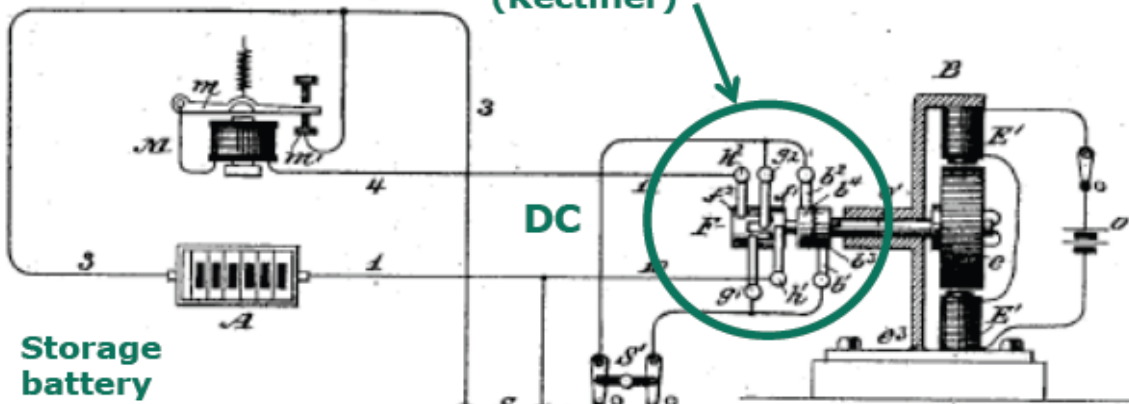
Application filed February 4, 1887. Serial No. 226,408. (No model.)

# AC-DC Origins...

Electro-magnetic cut-out

Rectifying commutator  
(Rectifier)

AC Generator  
Alternate-current electric motor



Storage battery

DC

Switch

SYSTEM OF ELECTRICAL DISTRIBUTION  
1887

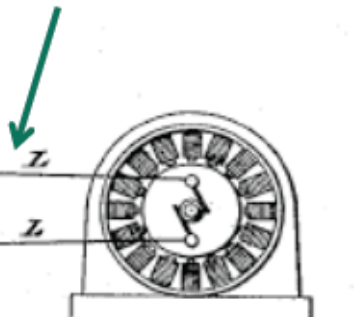
Main line

Incandescent lights  
AC / DC

Secondary line

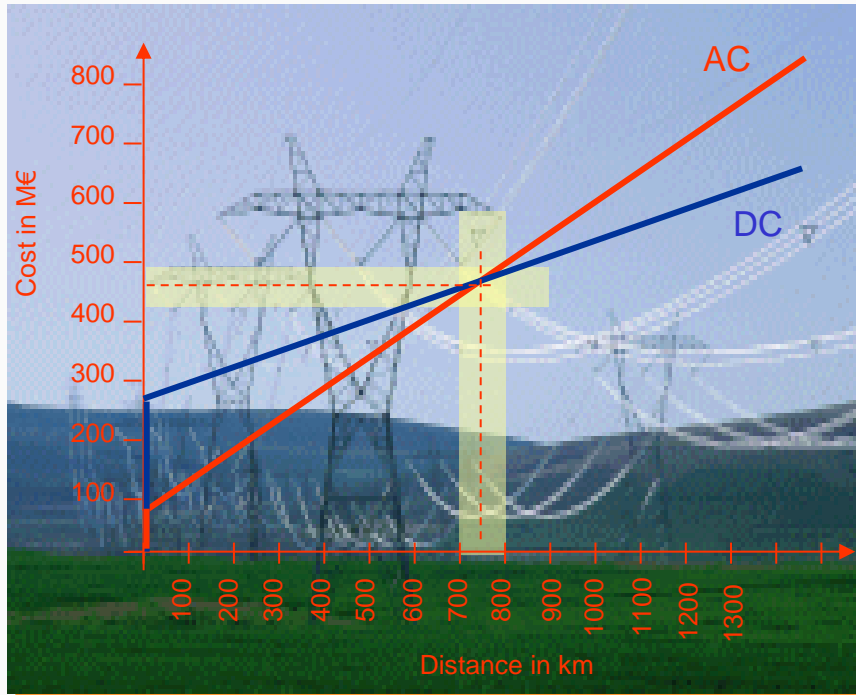
Converter  
(Transformer)

AC Generator



# HVDC - Costs and Solutions

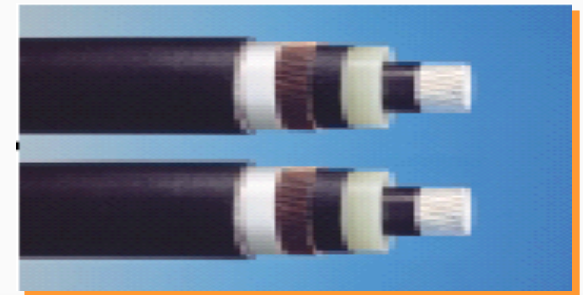
Cost estimation of a 2GW link overhead lines



High Voltage Direct Current. To transfer power from one point to another or to connect asynchronous grids.

Some hundreds installation in the world: it is a mature technology, for thyristor based solutions.

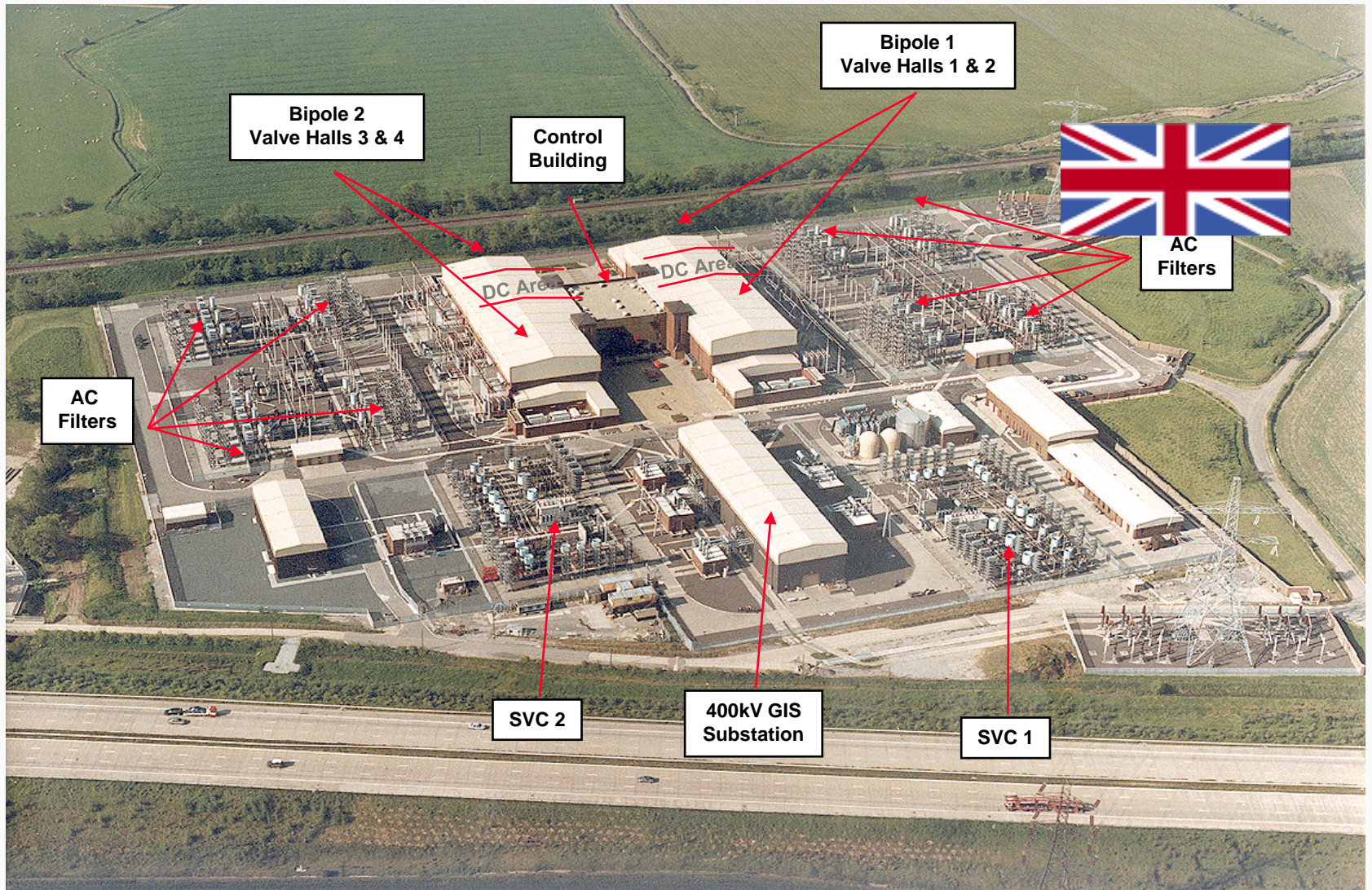
For Sea cables, the point of equality between AC and DC is obtained for shorter distances, as small as 30 km.



Courtesy: Alstom

# Interconnexion France Angleterre - IFA2000

## English side - SELLINDGE



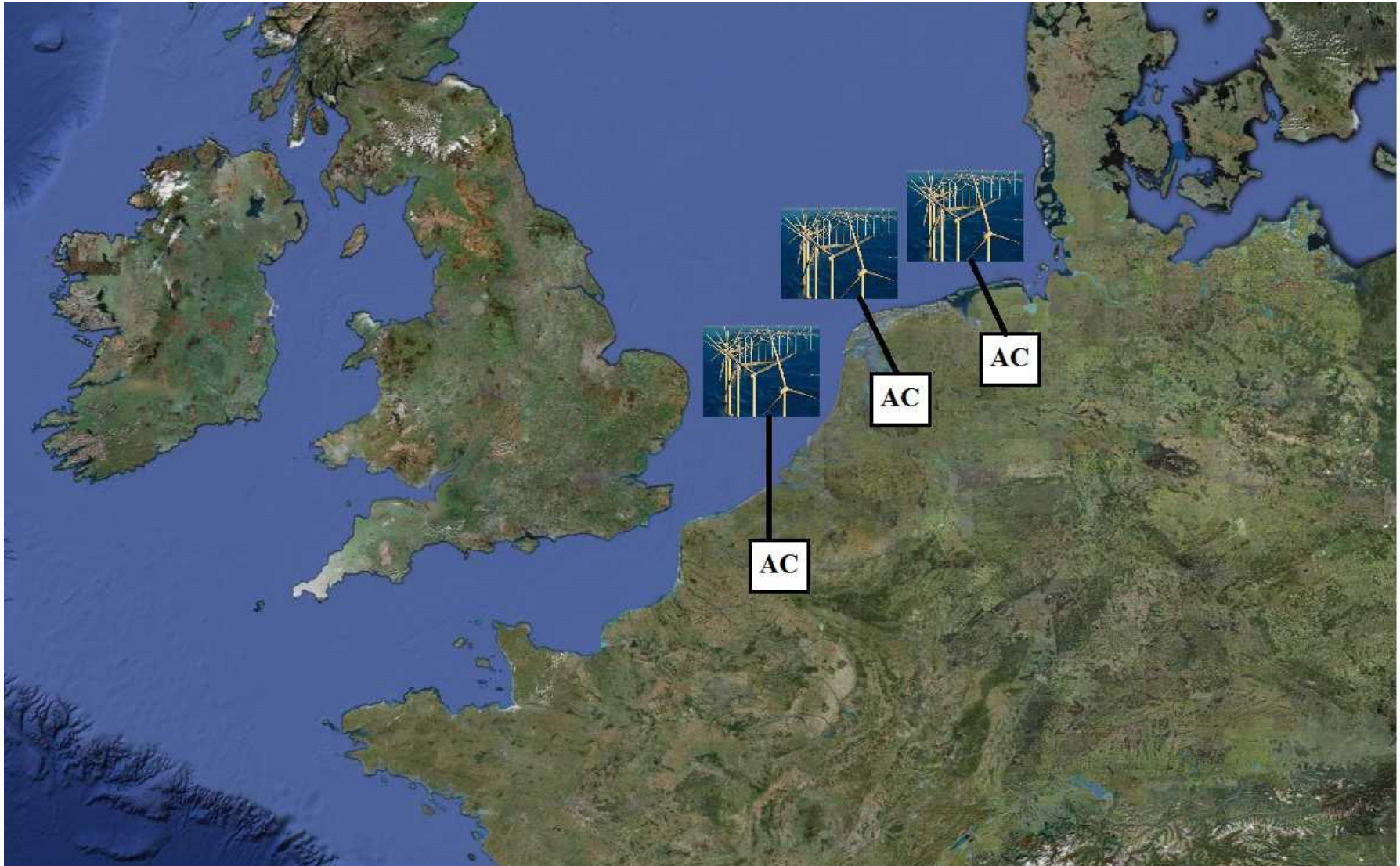
Courtesy: Alstom

# *Winpower*

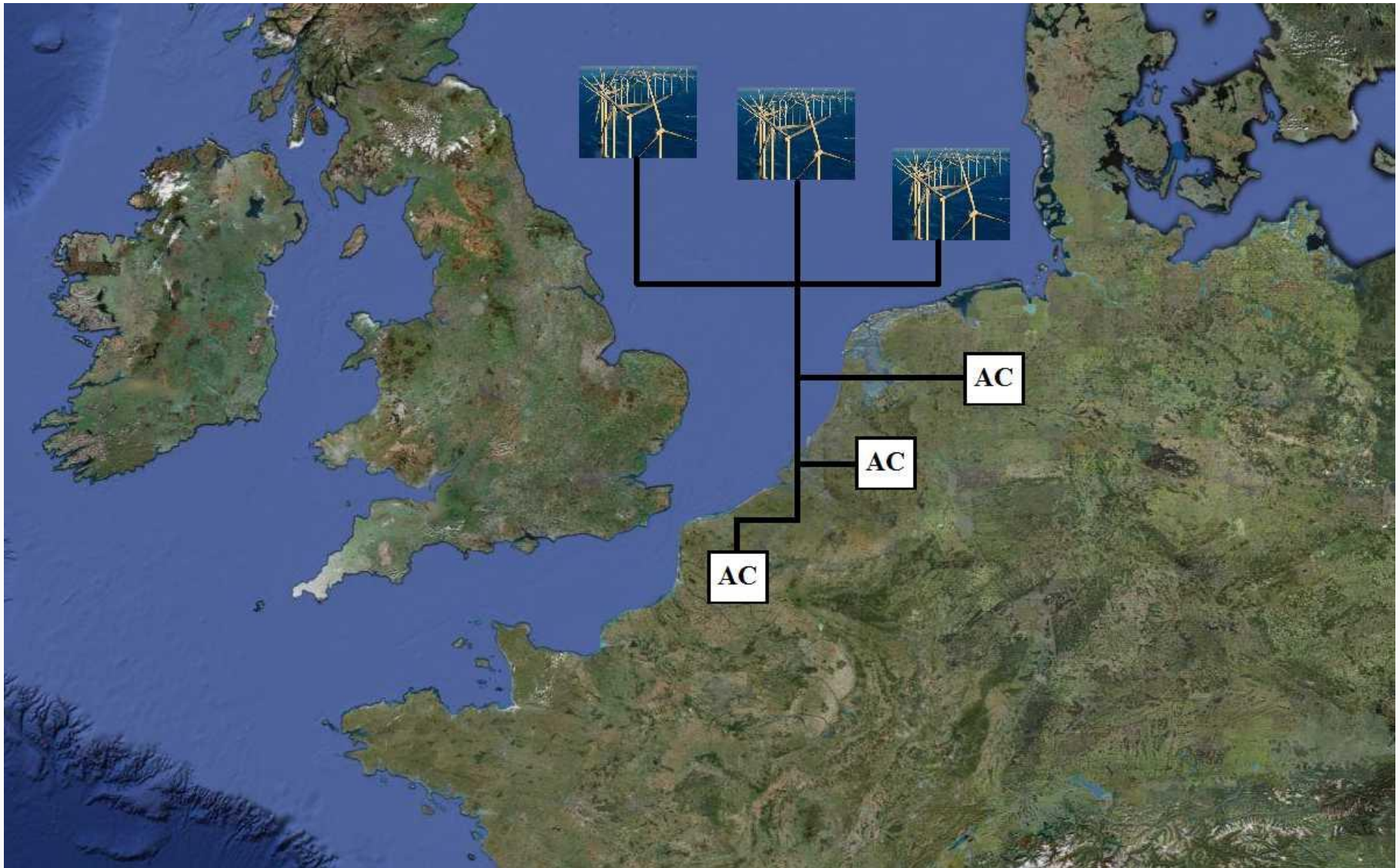
# *Multi-point HVDC*



# Multi-point HVDC

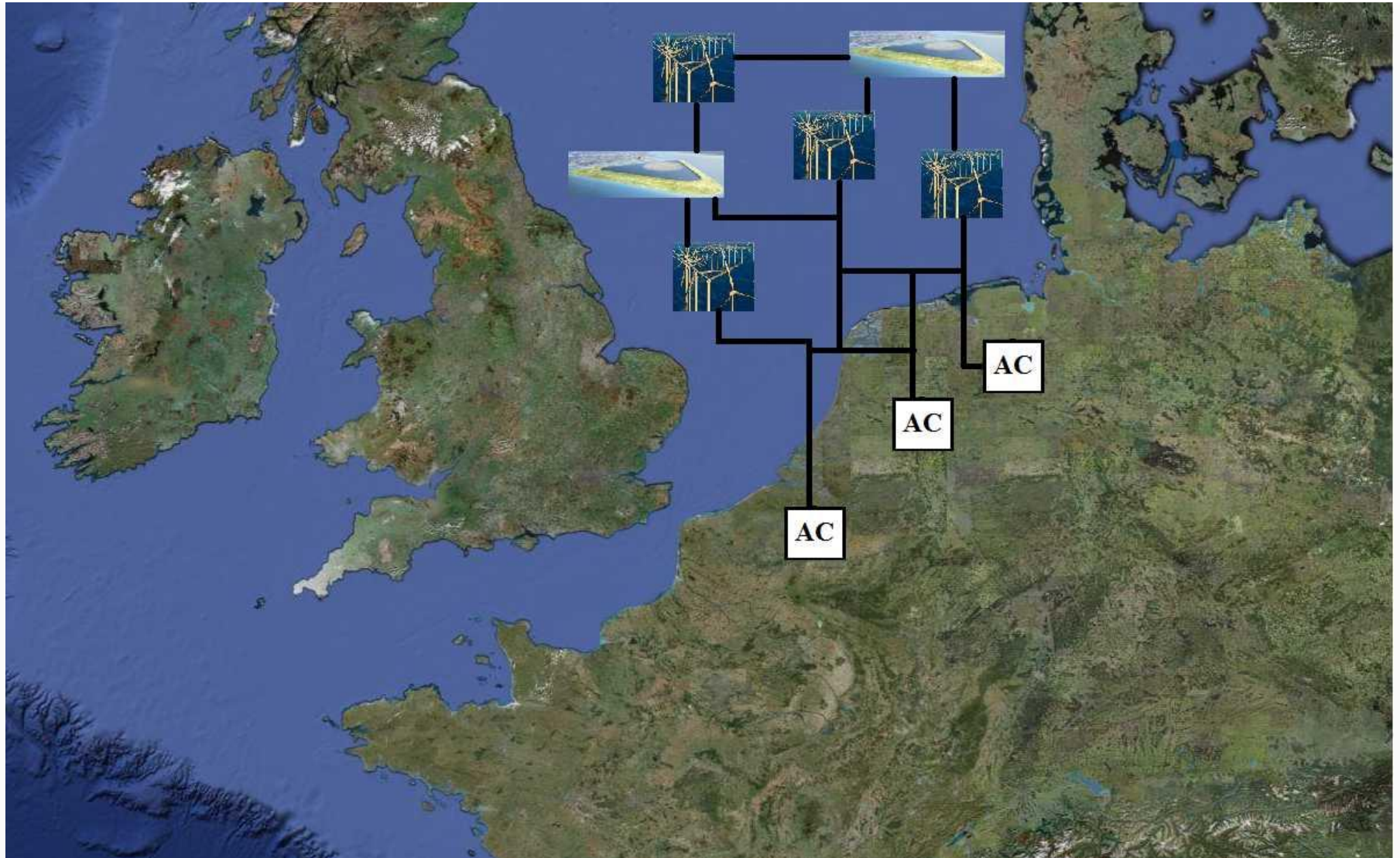


# Multi-point HVDC





# Multi-point HVDC

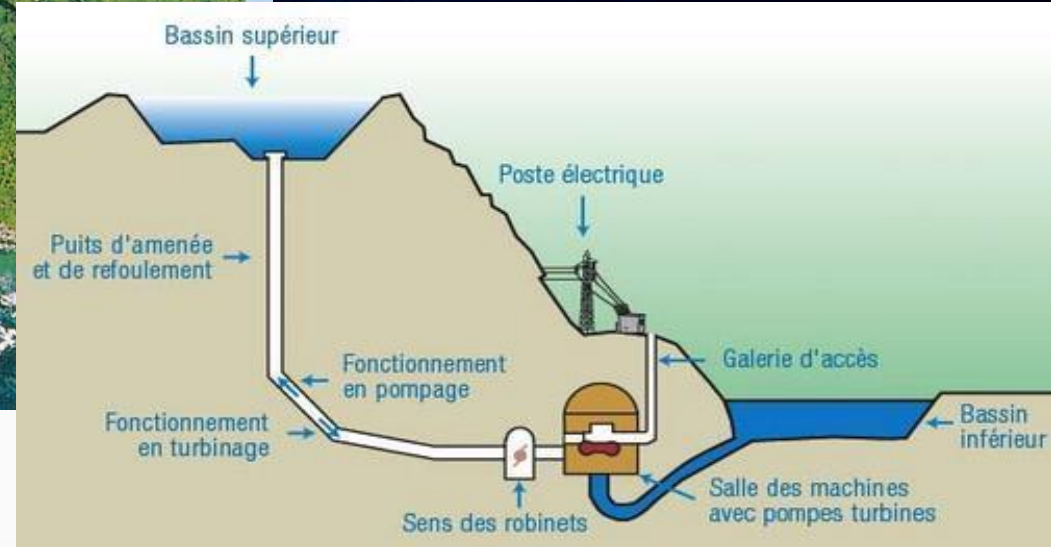


# *Multi-point HVDC - Converters*



# Storage – present → pumped water

Station en Okinawa

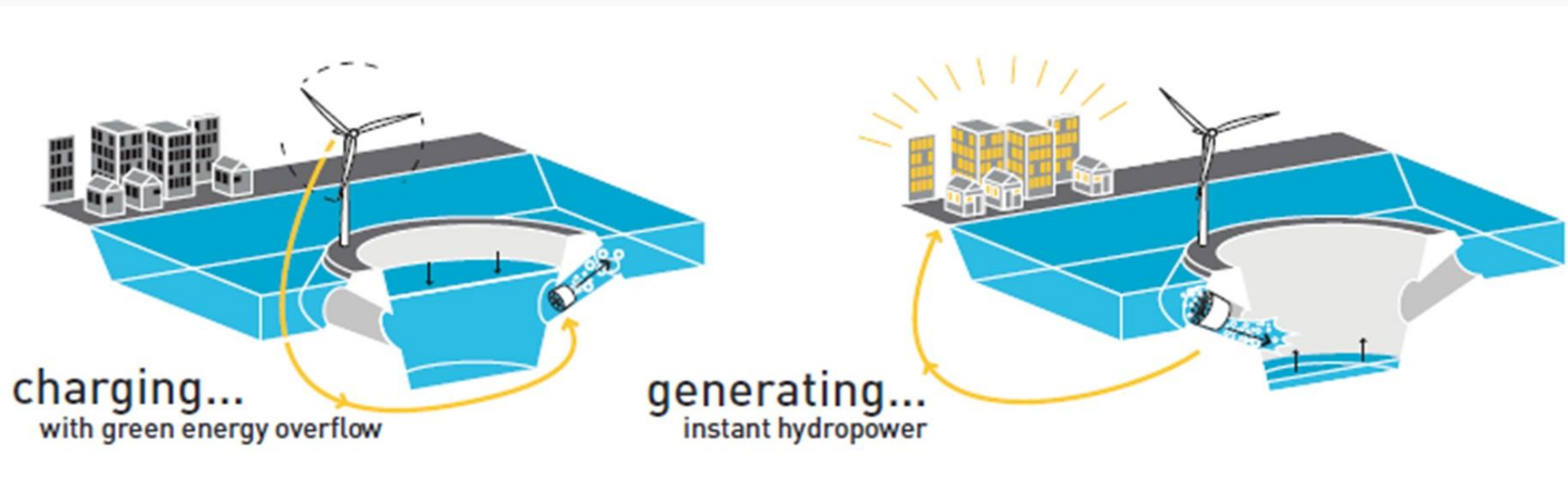


# Storage – future?

Project in Denmark



Project in Florida



# *Main ideas of Winpower: Model and control of meshed DC networks based on AC networks*

## ■ «Think globally, act locally »

- Main idea behind AC network deployment since the 30's
- Complex models (chaotic, fractals, distributed...)
- System of systems

## ■ Approach plug & play

- Adapt the system in real time
- Different spatial-temporal scales for decoupling and system's hierarchy
- Reconstruct an equivalent to inertia on DC by power electronics and storage

## ■ Winpower method – strong industrial academia combination and partnership

- Continuous evolution of simulation models and softwares
- Modularity
- Integration of sub-systems and their control laws in these modules

# *Design a control strategy based on the same concepts of AC grids → easier compatibility and integration*

## **AC Transmission Network frequency control & tools (same for voltage control)**

**Local control (ms)** - Generator control, node

**Primary control (s)** – global control but applied in a distributed way

Real time control via droop – each generator (node) is assigned with static gain ( $k_i$ ) and is assigned (by higher level) an amount of power to inject into the grid →  $\Delta P = k_i \times \Delta F$

**Secondary control (mn)** – global control – for  $F = F_{ref}$ , new references calc. →  $P_i = P_i'$

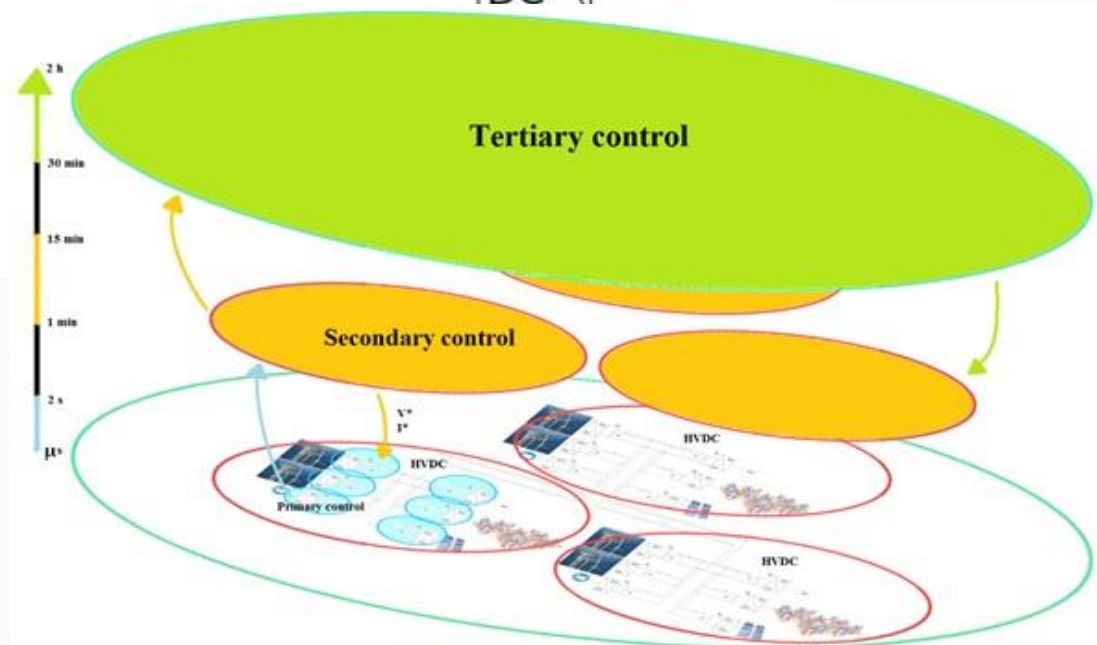
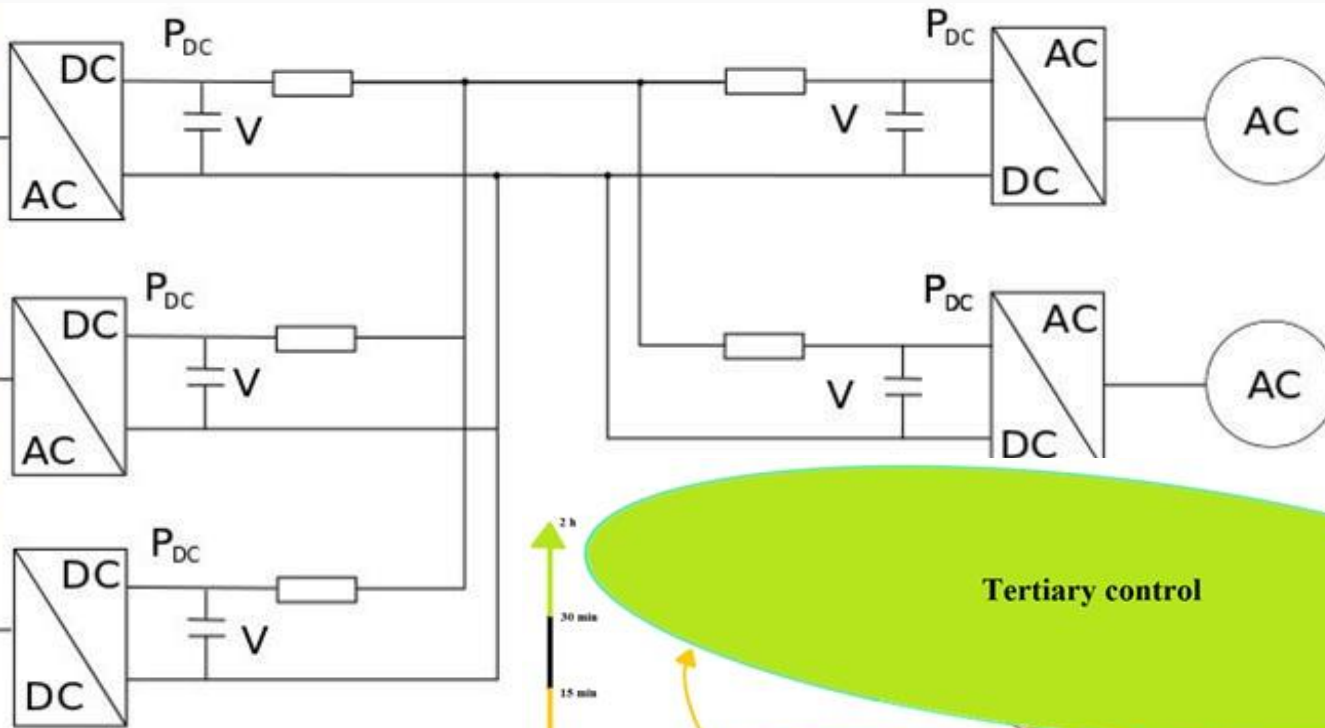
**Tertiary** – dispatching and Load shedding

**Plug & Play system already exists in AC network**

## **Use of AC control design and tools**

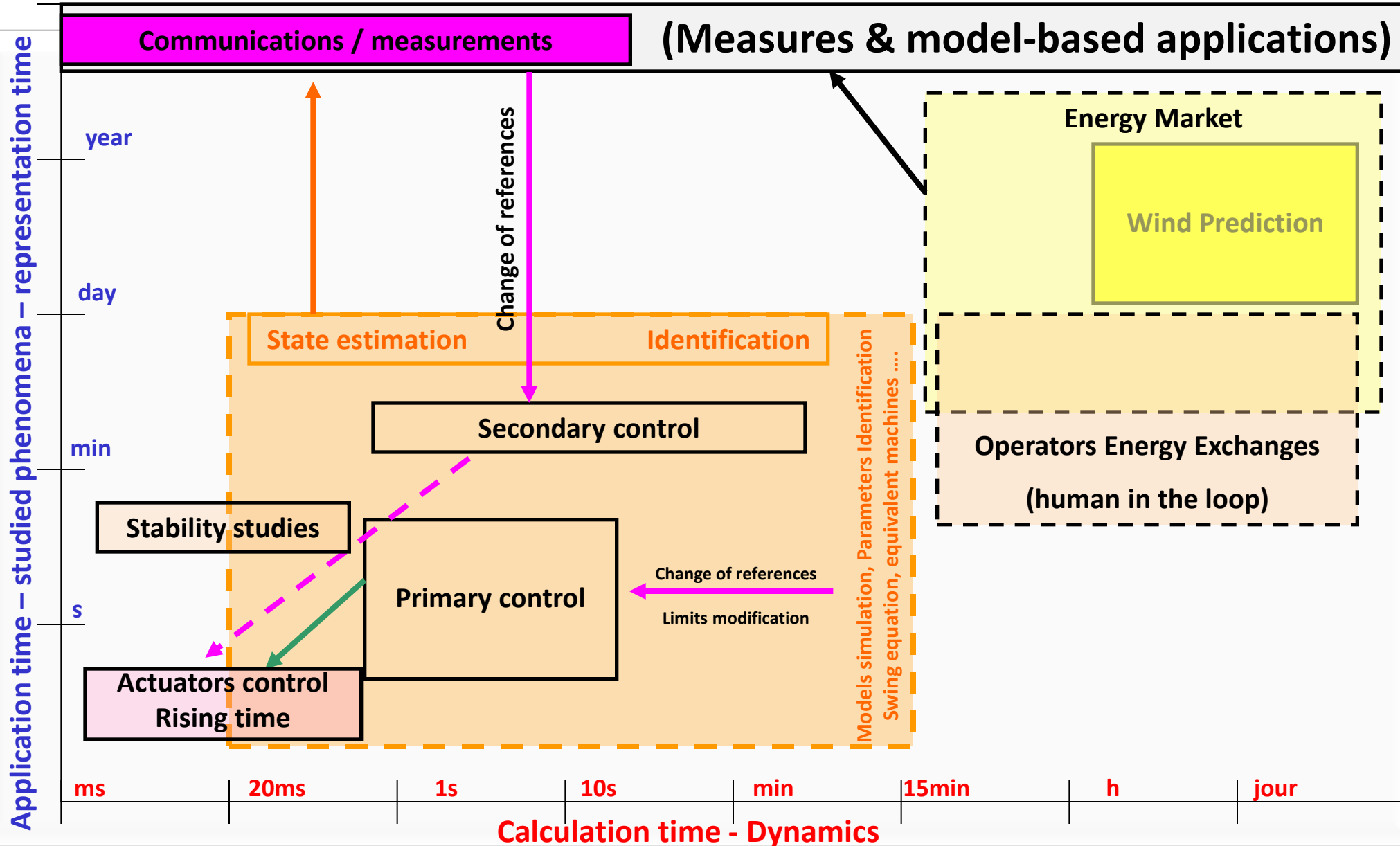
- ✓ Modeling large-scale systems – complex systems
- ✓ Machine equivalent model – swing equation/frequency for AC – capacitors and power electronics/voltages for DC

# Multi-point HVDC





# Time scale decoupling



# *Control of MT-HVDC Networks*

# *Operation of MTDC with loss minimization: Secondary control strategies*

LEVEL CONTROL	AC definition	WINPOWER definition
Level 3 (15 mn)	Tertiary	Tertiary
Level 2 (~ mn)	Secondary Control (U, $\Phi$ )	Secondary Control (~ mn)
	Primary Control (Droop)	Droop Control (P, I)
Level 1 (~ 10-20 ms)	Local control (PSS/ AVR of rotors, filters)	Local control (U) (converters, influence of cables, etc.)
Level 0	Protection	Protection (Outside of the study of Winpower)

# Secondary control objectives

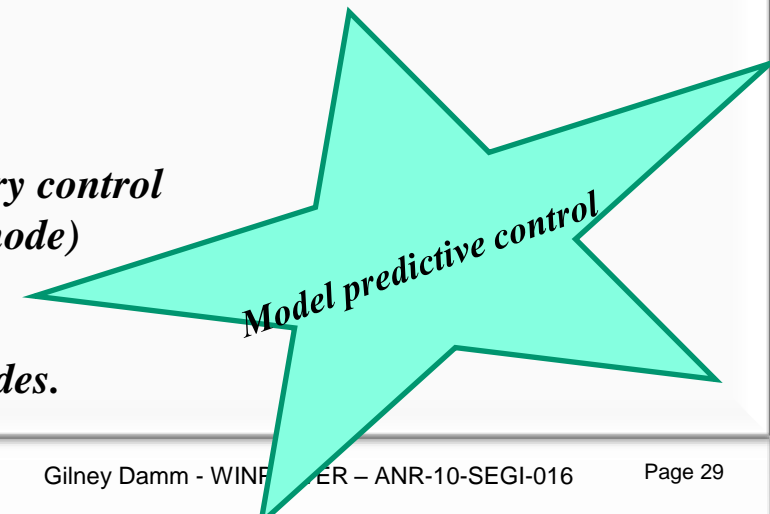
- *Follow tertiary planning references (who has already considered weather forecast ,electricity market ... ).*
- *Optimal Power flow coordination.*
  - *Optimized to minimize power losses in the lines*
  - *Optimized to minimize line congestion*
  - *Optimize to maximize profit*
  - *Optimize to reduce voltage variations*
  - *...*
- *Storage management.*
- *Prevent congestion on lines.*

## After disturbance:

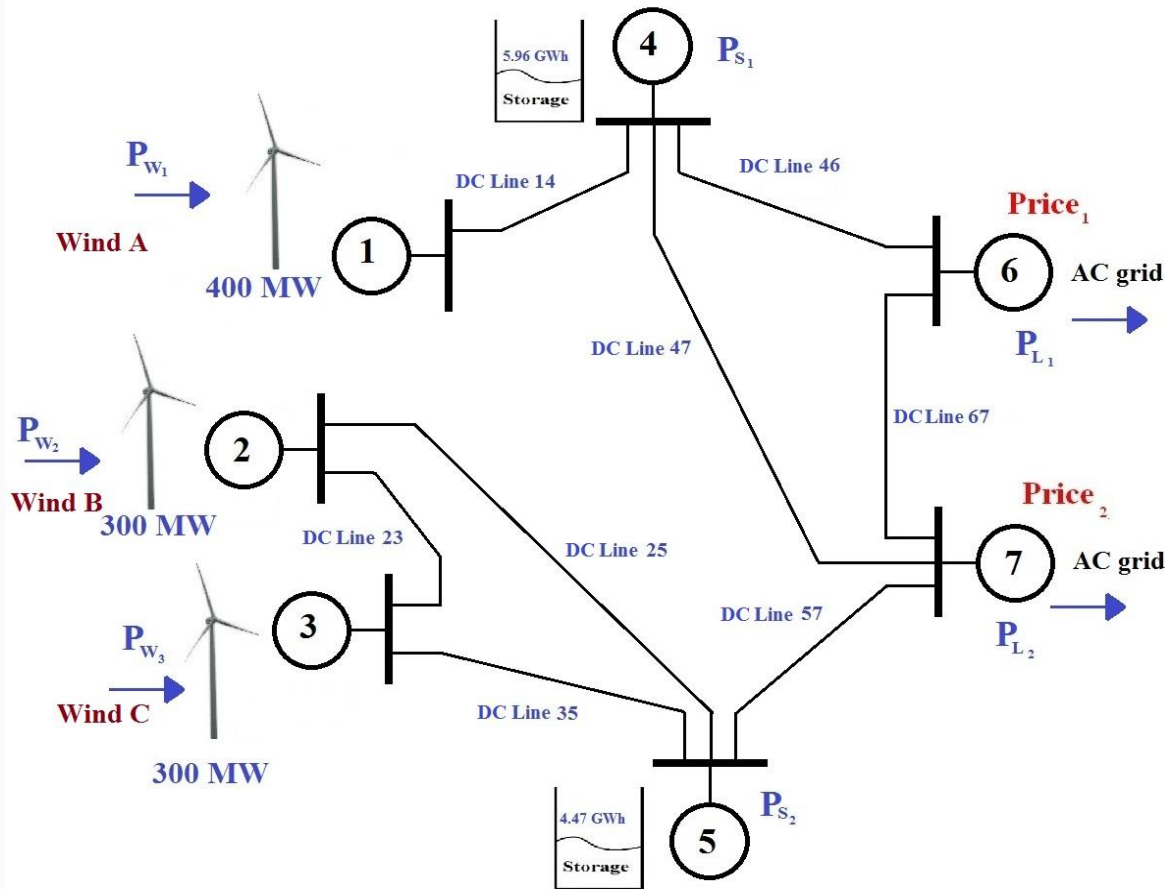
- *Get a level of stable non-degraded operation state*  
*Determine a new level of voltage*
- *Restore energy capacity of each storage node*
- *Re-dispatch the parameters of nodes in primary control*  
*(redistribute droop gains for each concerned node)*



*Communication is required between nodes.*



# Multi-point HVDC



## Secondary control

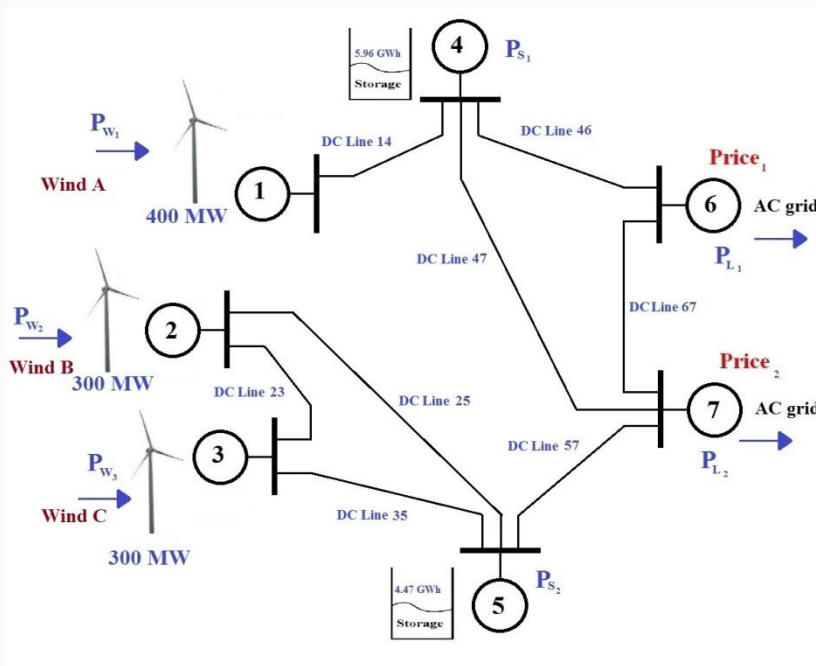
- *Secondary Control will command power flow within the network.*
- *Actuation time between 1 and 15 min.*
- *Storage size and response characteristics will determine the overall system performance.*

## Model Predictive control

Objective function

$$\min \left( \sum P_i \right) = \min([u]^t \cdot [Y] \cdot [u])$$

Subject to:



a)  $j \in A, B, E, F / P_j = [u]^t \cdot [Y]_j^* \cdot [u]$

b)  $P_{A,B} - P_{E,F} = P_{C,D} + P_{Losses}$

$P_{A,B} \equiv$  Generator nodes

$P_{C,D} \equiv$  Storage nodes

$P_{E,F} \equiv$  Consumption nodes

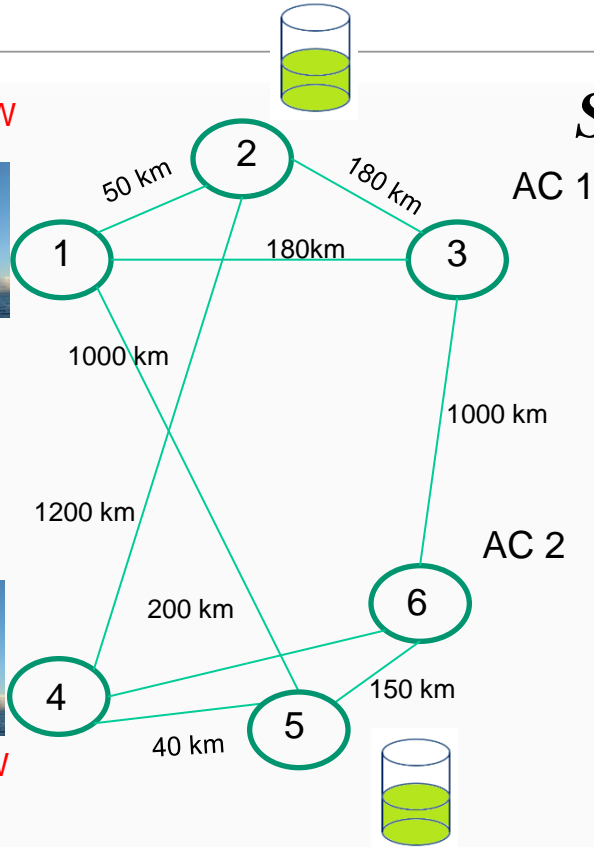
c)  $\frac{|u_i - u_j|}{R_{ij}} \leq I_{\max \text{ line } ij}$

d)  $u_{i,\min} \leq u_i \leq u_{i,\max}$

e)  $P_{C,D \min} \leq P_{C,D} \leq P_{C,D \max}$

# Secondary control - Results

400 MW



300 MW

## Simulations parameters

Line	$\Omega/\text{km}$
1-2	0.0121
1-3	0.0121
1-5	0.0121
2-3	0.0121
2-4	0.0121
3-6	0,0121
4-5	0.0121
4-6	0.0121
5-6	0.0121

Nominal voltage grid

100 kV

Base power

400 MW

$I_{\max}$

1 p.u.

Voltage

$0,9 \leq u_i \leq 1,1$  (p.u.)

$N_p$

2 hours

T

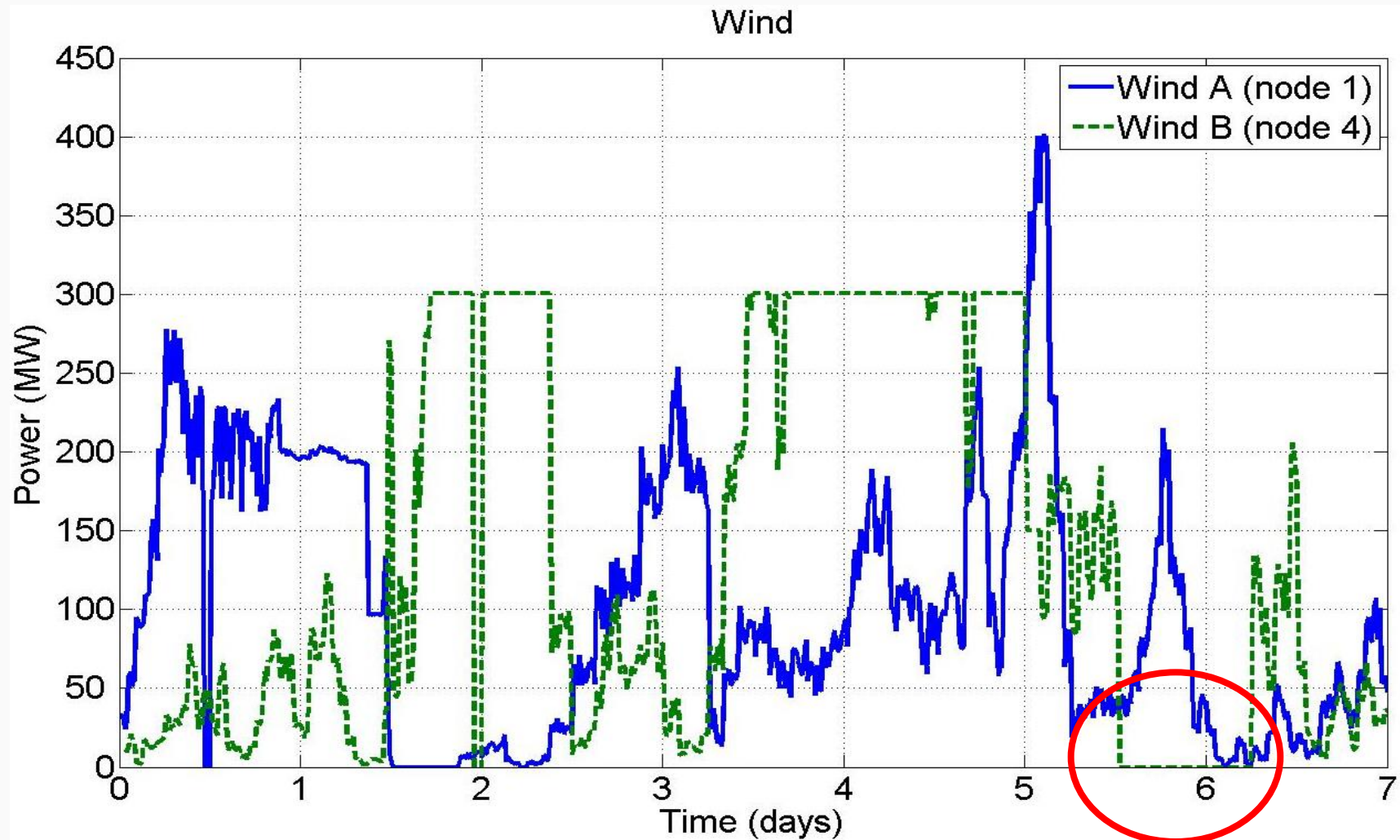
5 minutes

	Storage node 2	Storage node 5
Initial energy	60 %	50%
Maximum energy	10 GWh	3 GWh
Maximum power charging	350 MW ( $\eta=0,8$ )	220 MW ( $\eta=0,8$ )
Maximum power discharging	300 MW ( $\eta=0,85$ )	200 MW ( $\eta=0,85$ )

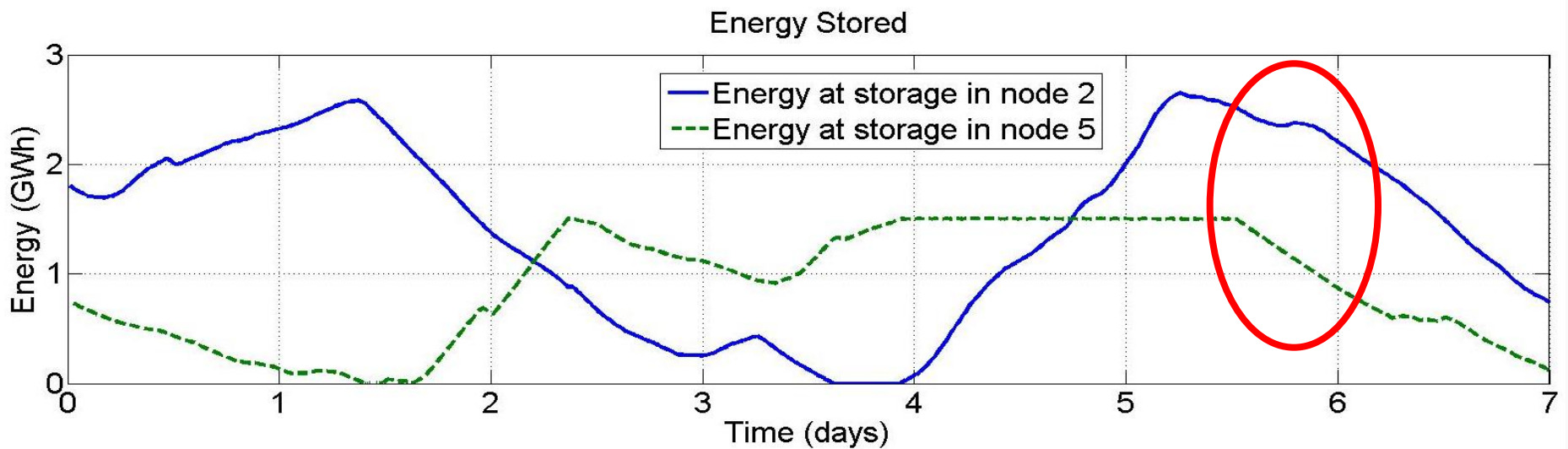
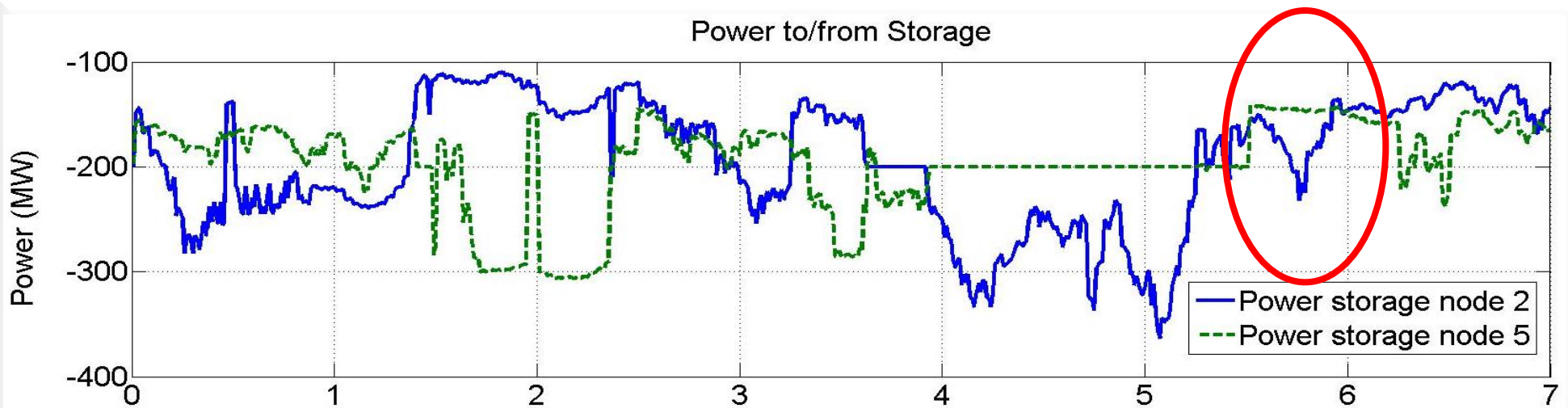


# Secondary control. Results.

## Simulations (b). Loss of generator node

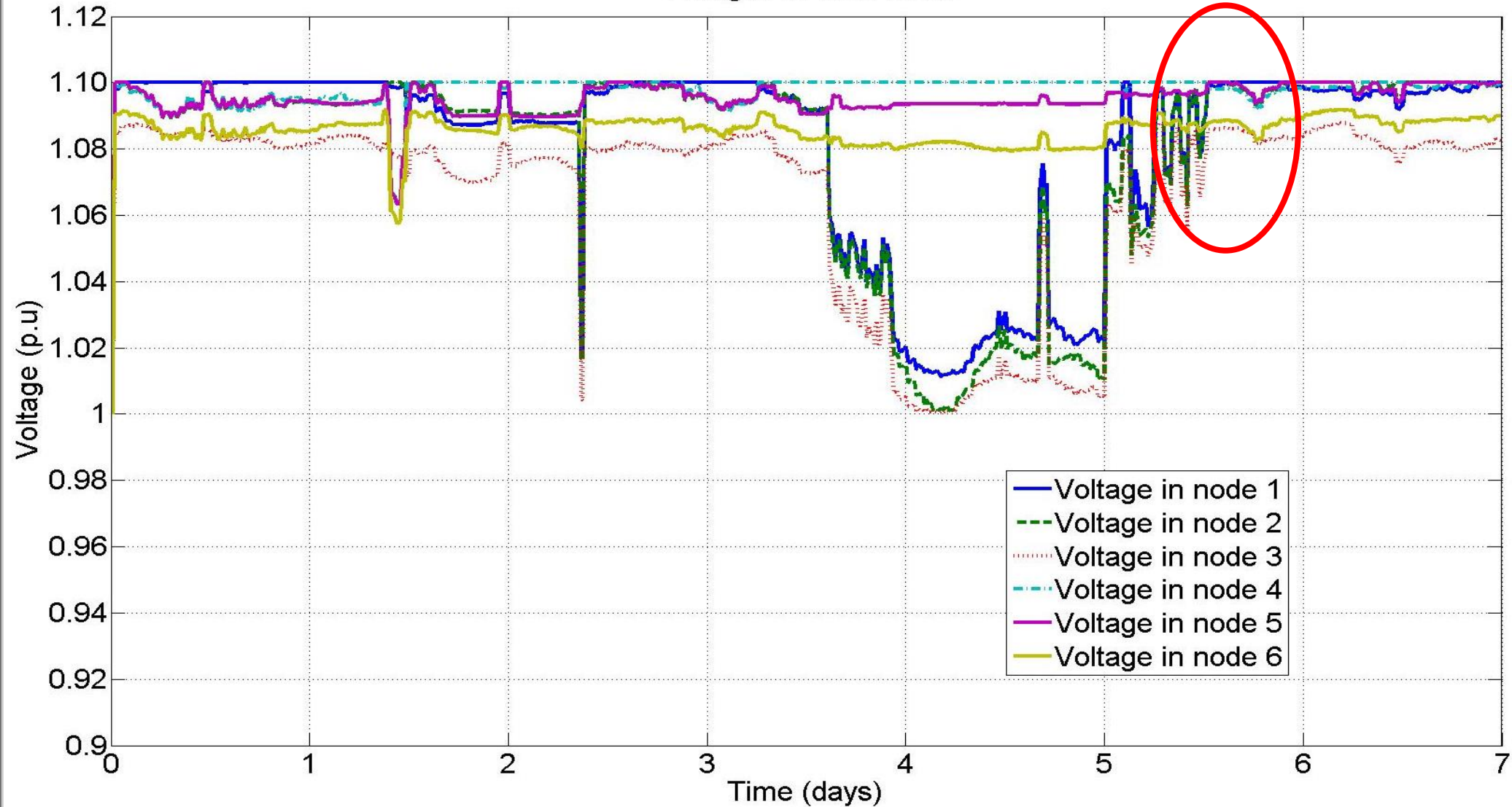


# Secondary control. Results.

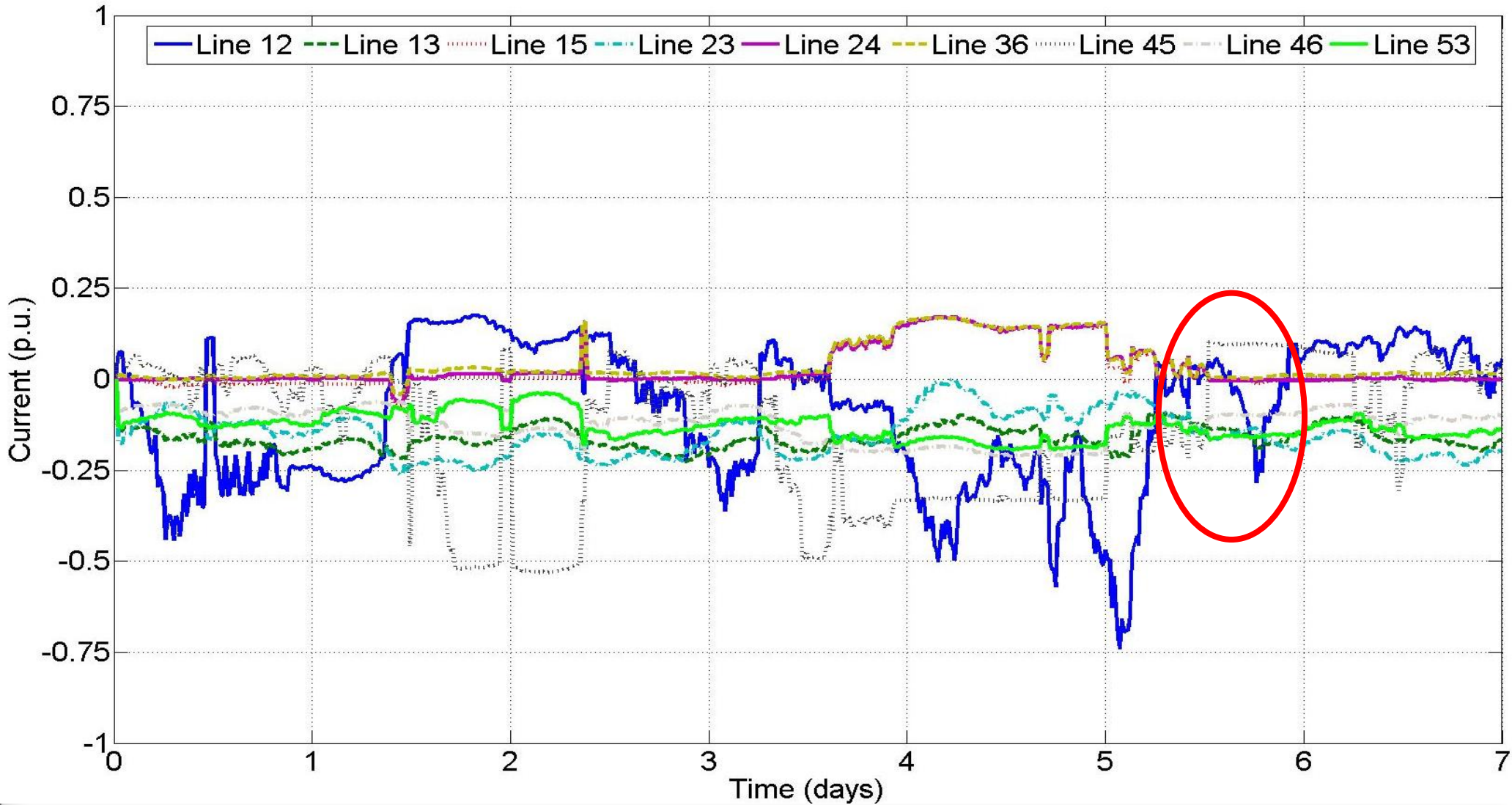


# Secondary control. Results.

Voltages in each node



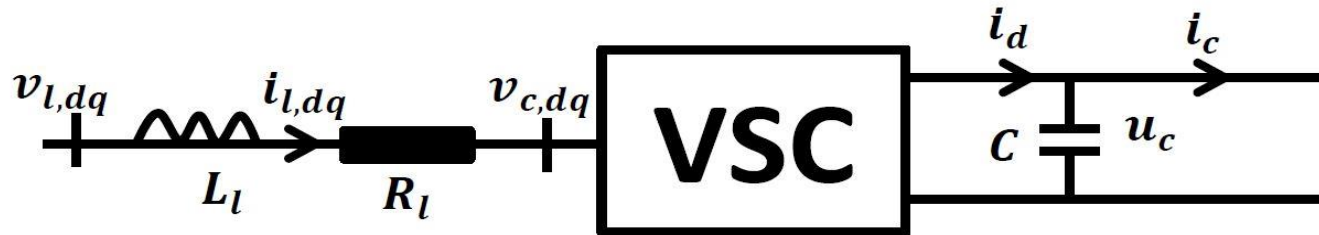
# Secondary control. Results.





# *Local Control of VSC converters – Stability analysis, methodologies*

# Specification of a converter



- A synchronous d-q reference frame is applied in stead of abc frame;
- $i_{ldq}$ : phase reactors currents;  $v_{ldq}$ : connected AC area voltage;  $v_{cdq}$ : converter voltage;  $C$ : DC capacitors;  $R_l, L_l$ : series connected phase reactors;  $u_c$ : DC voltage
- $i_c$ : measureable DC current representing an active demand or supply

# Modeling of a VSC-HVDC terminal

## State space model

$$\begin{aligned}\frac{di_{ld}}{dt} &= -\frac{R_l}{L_l}i_{ld} + \omega i_{lq} - \frac{1}{2L_l}M_d u_c + \frac{v_{ld}}{L_l} \\ \frac{di_{lq}}{dt} &= -\frac{R_l}{L_l}i_{lq} - \omega i_{ld} - \frac{1}{2L_l}M_q u_c + \frac{v_{lq}}{L_l} \\ \frac{du_c}{dt} &= -\frac{1}{C}i_c + \frac{1}{C}\frac{3}{4}(M_d i_{ld} + M_q i_{lq})\end{aligned}$$

$$P_l = \frac{3}{2}v_{ld}i_{ld}$$

$$Q_l = -\frac{3}{2}v_{ld}i_{lq}$$

dq reference frame make:  $v_{ld} = v_{l,rms}$  and  
 $v_{lq} = 0$

- State variables:  $i_{ld}$   $i_{lq}$   $u_c$ ;
- Control variables:  $M_d$   $M_q$  (modulation index)  
$$v_{c,dq} = \frac{1}{2}M_{dq}u_c$$
- External signal:  $i_c$
- System known parameters:  $R_l$   $L_l$   $v_{l,dq}$  and  $C$

## ❖ Develop different control structures :

- ❖ Make the DC voltage  $u_c$  and the reactive power  $Q_l$  track their desired values  $u_c^*$  and  $Q_l^*$  if  $i_c$  is subjected to certain changes
- ❖ Providing  $i_{lq}^*$  instead of  $Q_l^*$

## ❖ Control methods:

- ❖ Backstepping-like nonlinear controller
- ❖ Static/dynamic feedback linearization controller
  - ❖ Globally stable passive controller



# ❖ Backstepping-like nonlinear controller

Control variables  
 $M_{dq}$

State feedback  
control law

Eliminate the error  
fast dynamics  
 $\tilde{i}_{lid}, \tilde{i}_{liq}$

Reactive power  
control offers  $i_{liq}^*$

DC voltage control  
offers  $i_{lid}^*$

$$\begin{cases} M_{di} = \frac{2L_{li}}{u_{ci}} \left( -\frac{R_{li}}{L_{li}} i_{lid} + \omega_i i_{liq} + \frac{1}{L_{li}} v_{lid} - u_{id} \right) \\ M_{qi} = \frac{2L_{li}}{u_{ci}} \left( -\frac{R_{li}}{L_{li}} i_{liq} - \omega_i i_{lid} + \frac{1}{L_{li}} v_{liq} - u_{iq} \right) \end{cases}$$

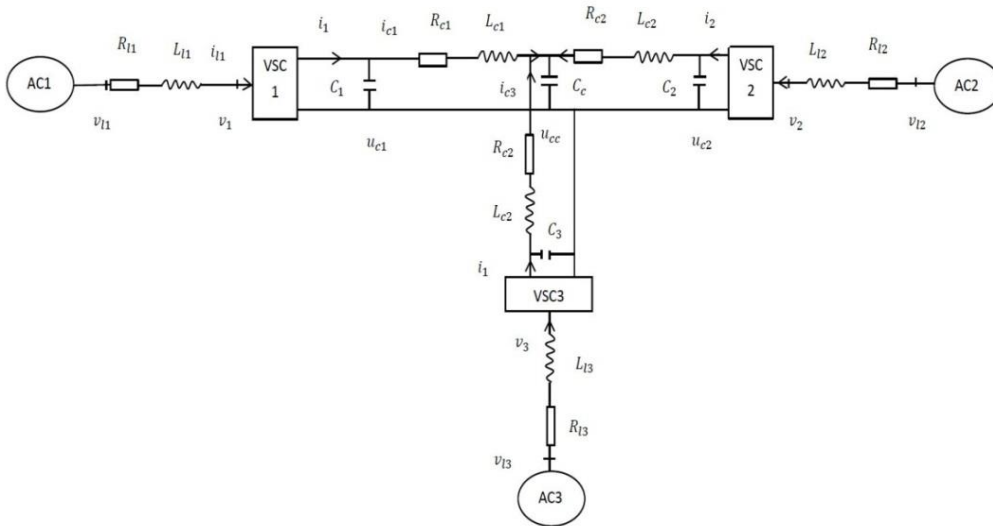
$$\begin{cases} u_{id} = \frac{di_{lid}}{dt} = \frac{\tilde{d}i_{lid}}{dt} + \frac{di_{lid}^*}{dt} \\ u_{iq} = \frac{di_{liq}}{dt} = \frac{\tilde{d}i_{liq}}{dt} + \frac{di_{liq}^*}{dt} \end{cases}$$

$$\begin{cases} \dot{\varphi}_{id} = \tilde{i}_{lid} \\ \tilde{i}_{lid} = -k_{id} \tilde{i}_{lid} - \lambda_{id} \varphi_{id} \\ \dot{\varphi}_{iq} = \tilde{i}_{liq} \\ \tilde{i}_{liq} = -k_{iq} \tilde{i}_{liq} - \lambda_{iq} \varphi_{iq} \end{cases}$$

$$i_{liq}^* = -\frac{2}{3} \frac{Q_{li}^*}{v_{lid}}$$

$$\begin{aligned} \frac{di_{lid}^*}{dt} = & -\frac{2}{3} \frac{u_{ci}}{i_{lid}} \frac{C_i}{L_{li}} \left( -k_{ci} \tilde{u}_{ci} - \lambda_{ci} \varphi_{ci} + \frac{i_{ci}}{C_i} \right) + \frac{u_{ci}}{2L_{li}} \frac{i_{liq}}{i_{lid}} M_{qi} \\ & + \left( -\frac{R_{li}}{L_{li}} i_{lid} + \omega_i i_{liq} + \frac{v_{lid}}{L_{li}} + k_{id} \tilde{i}_{lid} + \lambda_{id} \varphi_{id} \right) \end{aligned}$$

# Simulation results



Terminal	$R_{li}$	$L_{li}$	$R_{ci}$	$L_{ci}$
1	13.79 $\Omega$	31.02 mH	0.2085 $\Omega$	2.4 mH
2	12.79 $\Omega$	33.02 mH	0.2 $\Omega$	1 mH
3	13.57 $\Omega$	40.02 mH	0.235 $\Omega$	3.5 mH

Table 2.1: Parameter values of the terminals.

## A three-terminal VSC-HVDC transmission system

### Remark:

1.  $Q_{l1}^*$ ,  $Q_{l2}^*$  and  $Q_{l3}^*$  are set up to zero.
2. The feedback control gains:  
 $k_{id} = 100$ ,  $\lambda_{id} = 100$ ,  $k_{iq} = 100$ ,  $\lambda_{iq} = 100$ ,  $k_{ci} = 25$ ,  $\lambda_{ci} = 5$
3. Other parameters:  $\omega_i = 314$ ,  $C_i = 12\mu F$ ,  $v_{li} = 230KV$

# Simulation results

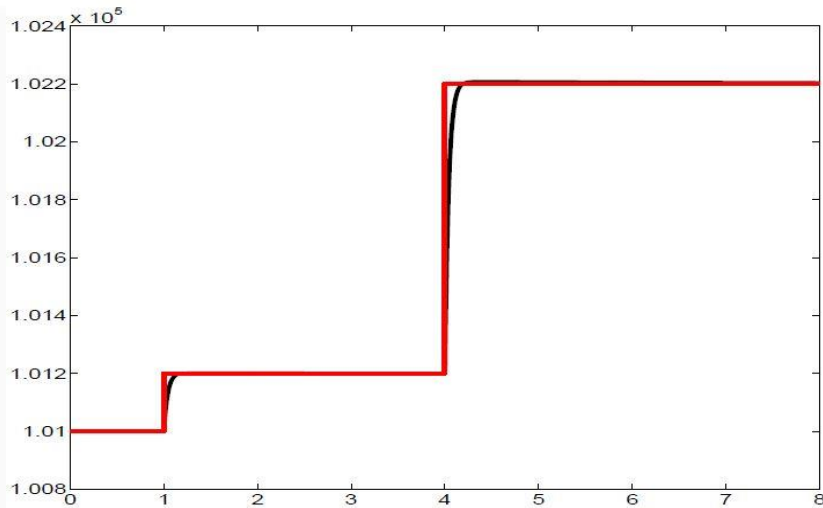


Fig. 4.  $u_{c1}$  response.

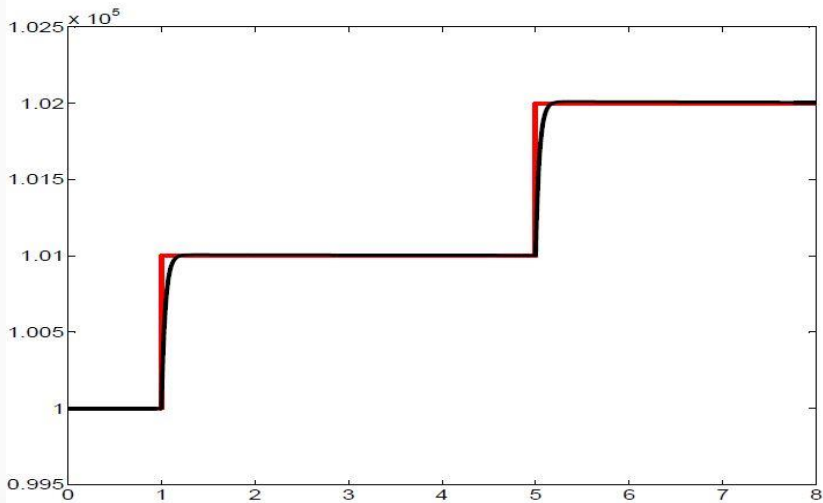


Fig. 6.  $u_{c2}$  response.

Time (s)	Event
0	$u_{c1}^* = 101$ kV, $u_{c2}^* = 100$ kV, $u_{c3}^* = 99.8$ kV
1	$u_{c1}^* = 101.2$ kV, $u_{c2}^* = 101$ kV, $u_{c3}^* = 99.9$ kV
4	$u_{c1}^* = 102.2$ kV
5	$u_{c2}^* = 102.0$ kV
6	$u_{c3}^* = 100.9$ kV

TABLE II

SEQUENCE OF EVENTS APPLIED TO THE SYSTEM.

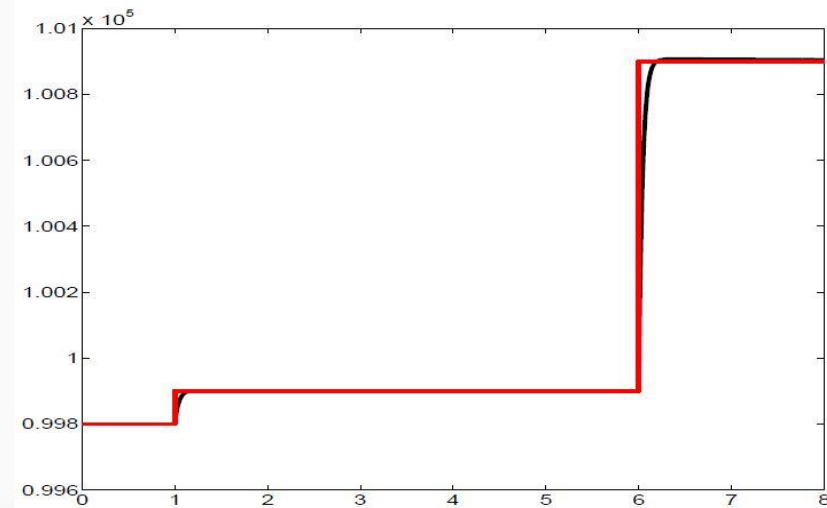


Fig. 8.  $u_{c3}$  response.



# ❖ Static/dynamic feedback linearization controller

$i_c < 0$  (inversion mode): static feedback linearization

Control variables  
 $M_{dq}$

$$\begin{pmatrix} M_d \\ M_q \end{pmatrix} = J^{-1} \begin{pmatrix} v_q - \left(-\frac{R_l}{L_l} i_{lq} - \omega i_{ld} + \frac{v_{lq}}{L_l}\right) \\ v_u - \left(-\frac{i_c}{C}\right) \end{pmatrix}$$

Additional inputs  
 $v_{qu}$

$$\begin{aligned} v_q &= \frac{di_{lq}^*}{dt} + k_{pq}(i_{lq}^* - i_{lq}) \\ v_u &= \frac{du_c^*}{dt} + k_{pu}(u_c^* - u_c) \end{aligned}$$

Zero dynamics:

$$A = \frac{1}{L_l} \frac{\frac{2}{3} u_c^* i_c - R_l (\bar{i}_{ld})^2}{(\bar{i}_{ld})^2} < 0$$

$$J^{-1} = \begin{pmatrix} \frac{2L_l i_{lq}}{u_c} & \frac{4C}{3i_{ld}} \\ -\frac{2L_l}{u_c} & 0 \end{pmatrix}$$

$$J = \begin{pmatrix} L_{g_d}(i_{lq}) & L_{g_q}(i_{lq}) \\ L_{g_d}(u_c) & L_{g_q}(u_c) \end{pmatrix}$$

$$\begin{aligned} L_{g_d}(i_{lq}) &= 0 \\ L_{g_d}(u_c) &= \frac{3i_{ld}}{4C} \\ L_{g_q}(i_{lq}) &= -\frac{u_c}{2L_l} \\ L_{g_q}(u_c) &= \frac{3i_{lq}}{4C} \end{aligned}$$

# ❖ Static/dynamic feedback linearization controller

$i_c > 0$  (rectification mode): dynamic-like feedback linearization

Control variables  
 $M_{dq}$

Additional inputs  
 $v_{dq}$

$i_{ld}^*$

$$\begin{pmatrix} M_d \\ M_q \end{pmatrix} = \frac{2L_l}{u_c} \begin{pmatrix} (-R_l i_{ld} + \omega L_l i_{lq} + v_{ld}) - v_d \\ (-R_l i_{lq} - \omega L_l i_{ld} + v_{lq}) - v_q \end{pmatrix}$$

$$v_d = \frac{di_{ld}^*}{dt} + k_{pd}(i_{ld}^* - i_{ld})$$

$$v_q = \frac{di_{lq}^*}{dt} + k_{pq}(i_{lq}^* - i_{lq})$$

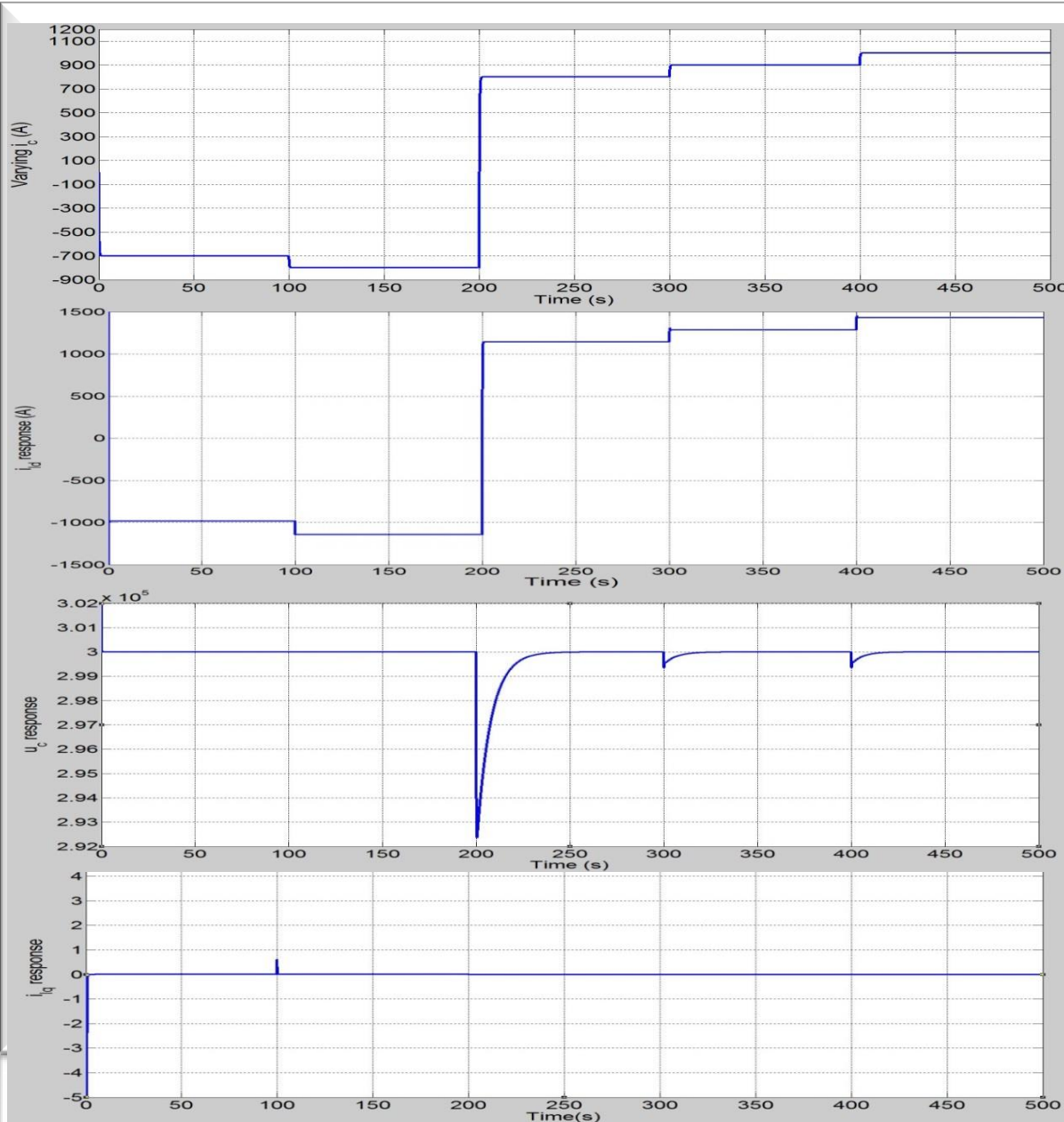
$$\frac{di_{ld}^*}{dt} = \frac{[-L_{f_0}^2(u_{c,re}) - c_1(u_{c,re} - u_c^*) - c_2 z_2]}{L_{g_0} L_{f_0}^1(u_{c,re})}$$

$$L_{f_0}^1(u_{c,re}) = -\frac{i_c}{C} + \frac{3}{2C} \times \frac{(-R_l i_{ld}^{*2} + v_{ld} i_{ld}^*) + (-R_l i_{lq}^{*2} + v_{lq} i_{lq}^*)}{u_{c,re}}$$

$$L_{f_0}^2(u_{c,re}) = -\frac{3\dot{u}_{c,re}}{2C} \frac{(-R_l i_{ld}^{*2} + v_{ld} i_{ld}^* + -R_l i_{lq}^{*2} + v_{lq} i_{lq}^*)}{u_{c,re}^2}$$

$$L_{g_0} L_{f_0}^1(u_{c,re}) = \frac{3}{2C} \frac{1}{u_{c,re}} (-2R_l i_{ld}^* + v_{ld})$$

# Simulation results



Terminal	$R_l$	$L_l$	$v_{ld}$	$C$	$f$
	0.05 $\Omega$	40e-3 H	140 kV	20e-3 F	50 Hz

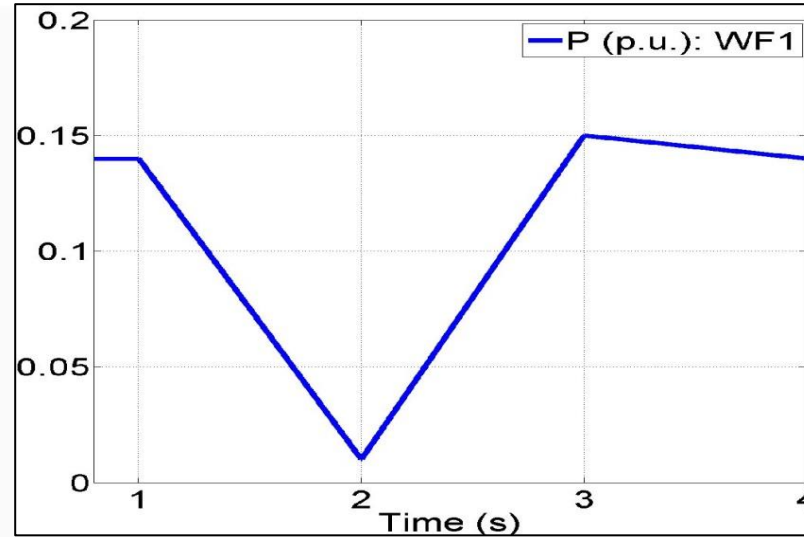
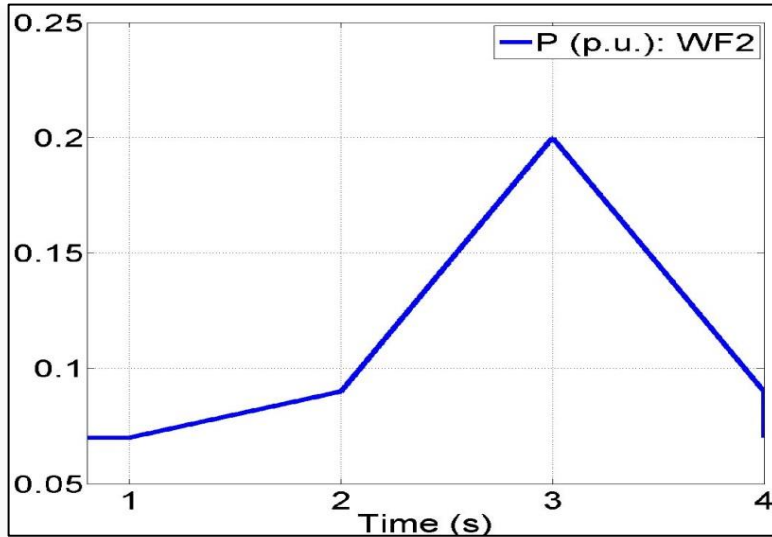
TABLE I  
PARAMETER VALUES OF THE VSC TERMINAL.

## Conclusion:

- Linear control theory can be applied to position new poles
- Control structure requires to switch between two control laws in different operation mode.



# Simulation results



- Power flows from WFs varying with respect to the wind speed

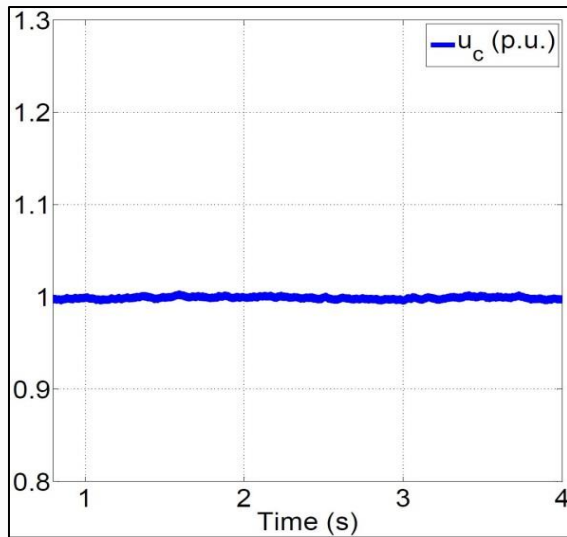
Active power generated by wind farms

## Control objective:

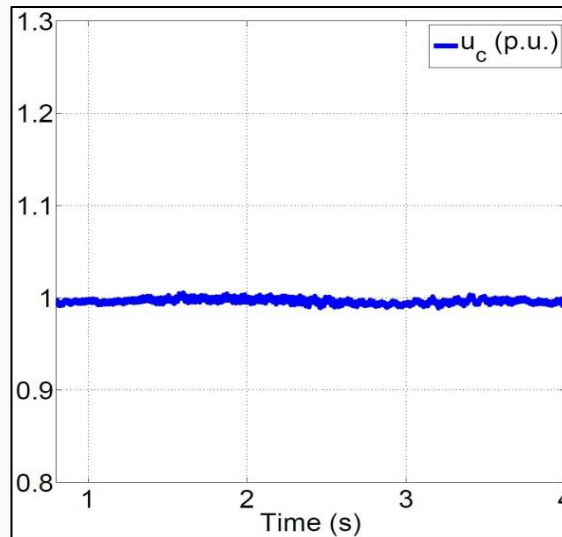
- Make all reactive powers follow the reference  $Q_i^* = 0$ ;
- Enable to tolerate the variations in power flows and always guarantee the DC voltage transmission level at the desired value  $u_c^* = 1$  p.u..
- Ensure the power flows generated by WFs being totally transferred.



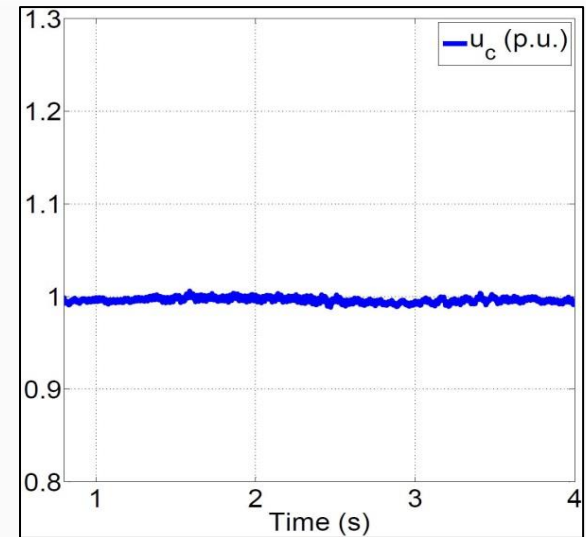
# Simulation results



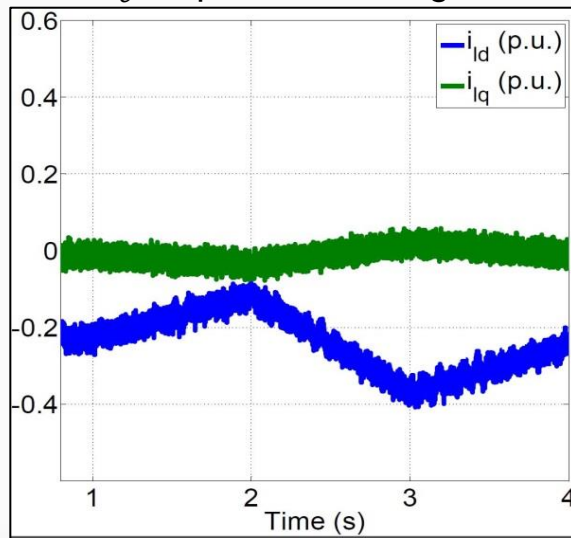
$u_c$  responses of AC grid



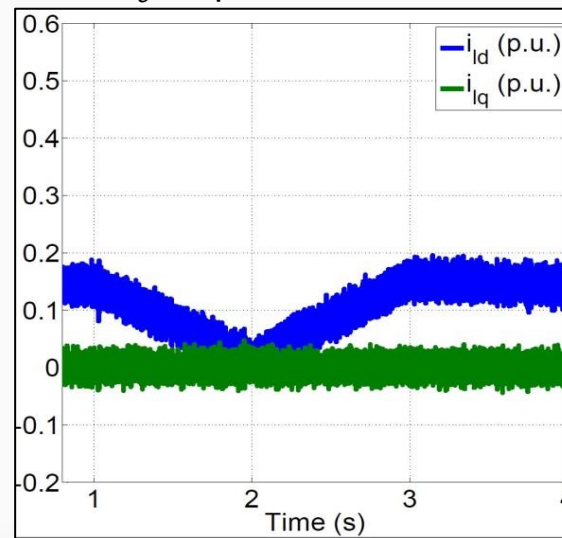
$u_c$  responses of WF1



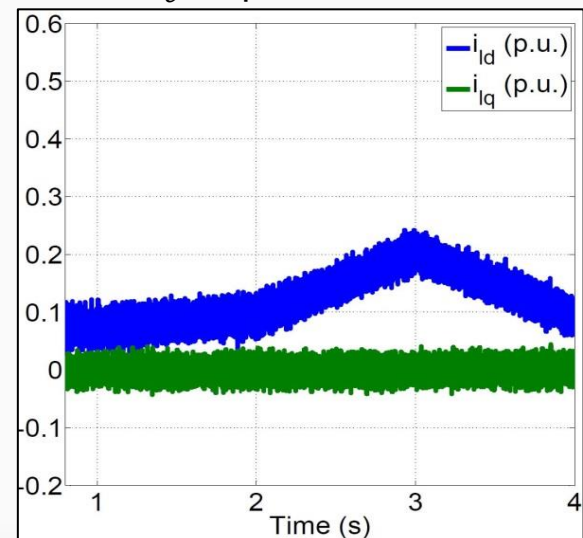
$u_c$  responses of WF2



$i_{l,dq}$  responses of AC grid



$i_{l,dq}$  responses of WF1



$i_{l,dq}$  responses of WF2

# Comparison between different approaches

- Stability:
- Power direction
- Linear system theory
- Need equilibrium point in advance

## Backstepping-like nonlinear controller

- Local
- Unidirectional
- Applicable
- No need

## Static/dynamic feedback linearization controller

- Local
- Bidirectional
- Applicable
- No need

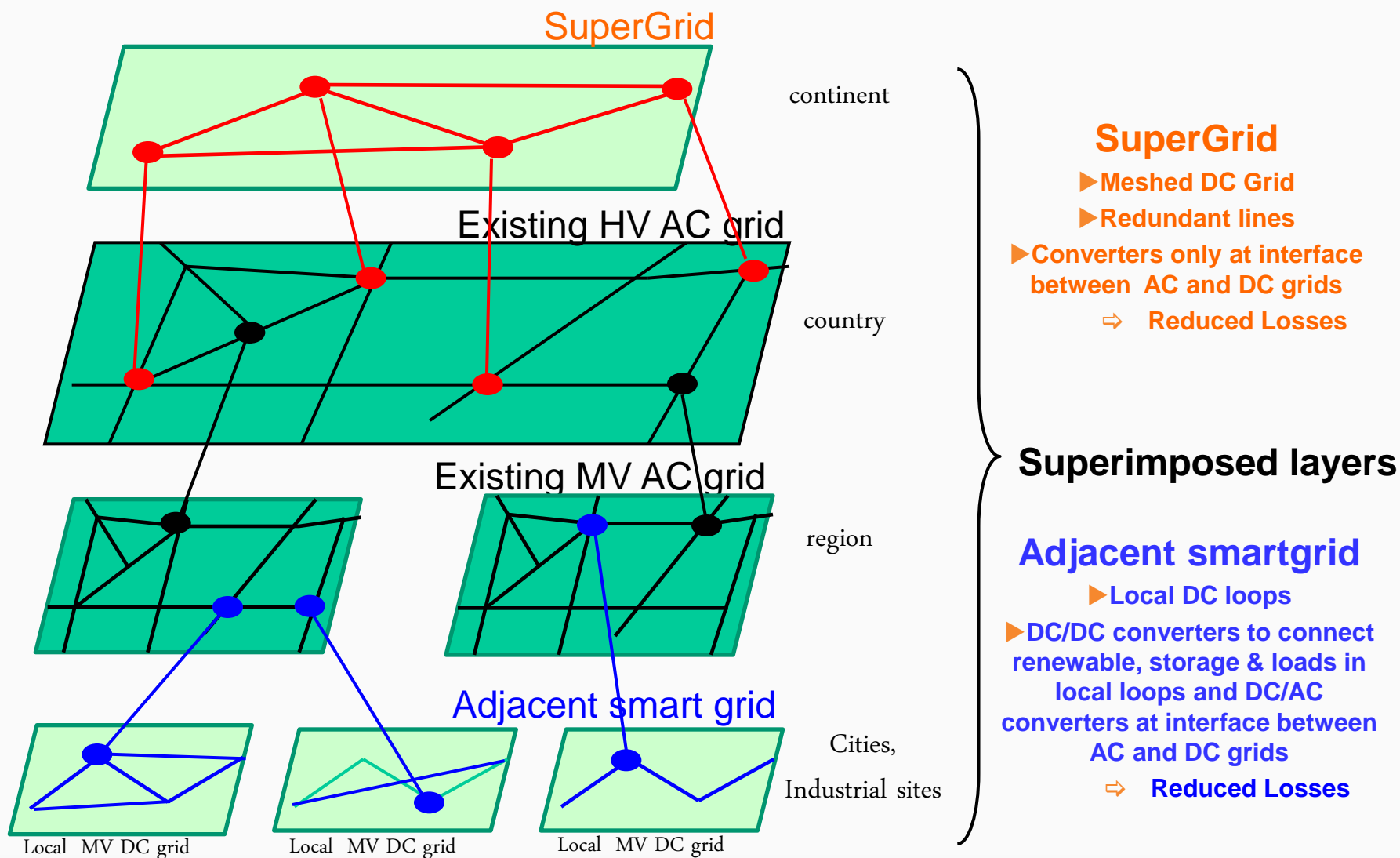
## Globally stable passive controller

- Global
- Bidirectional
- Non applicable
- Need

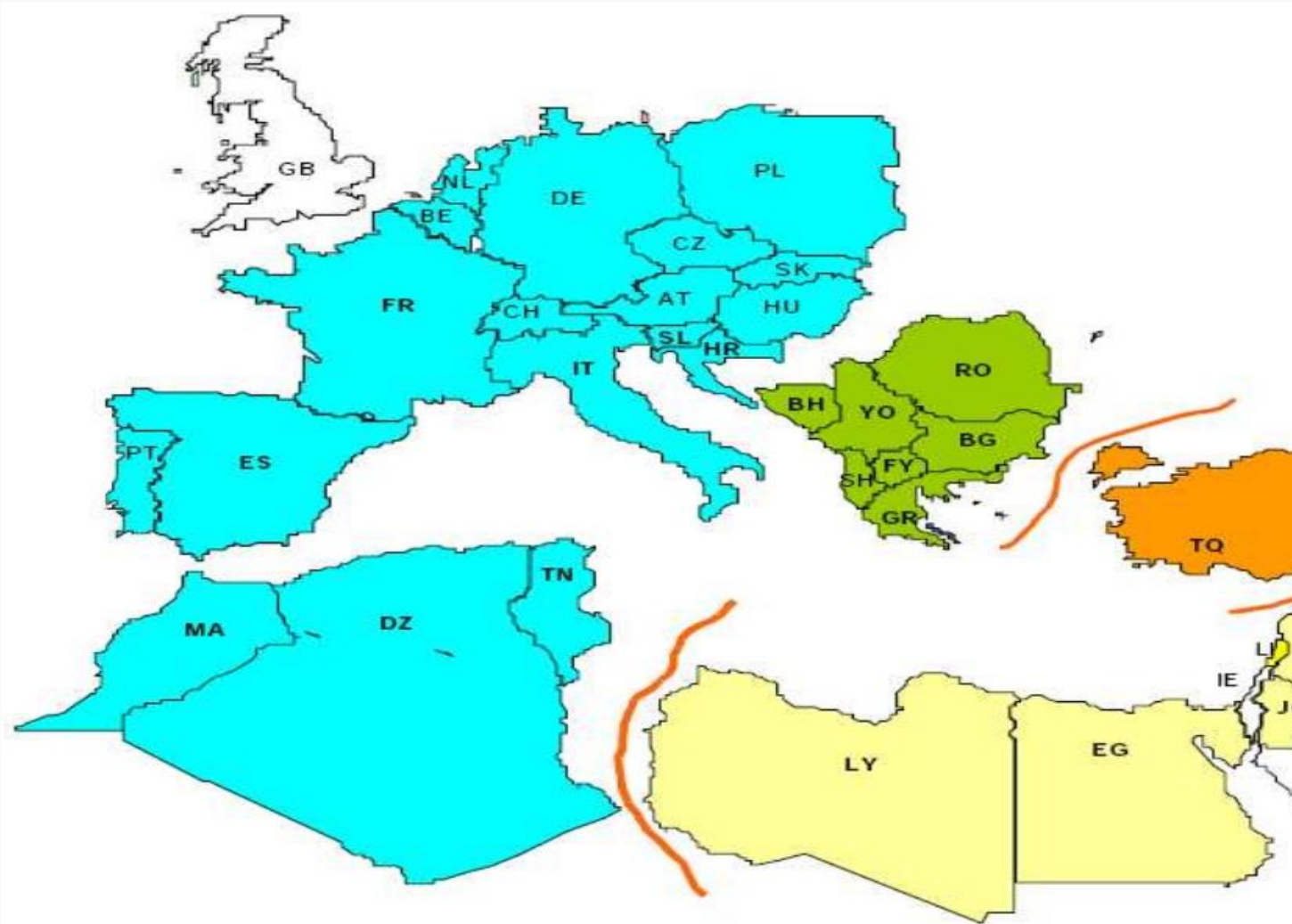
*Even further steps*

*Constructing a SuperGrid*

# 2020 vision: Supergrid & Adjacent Smartgrid



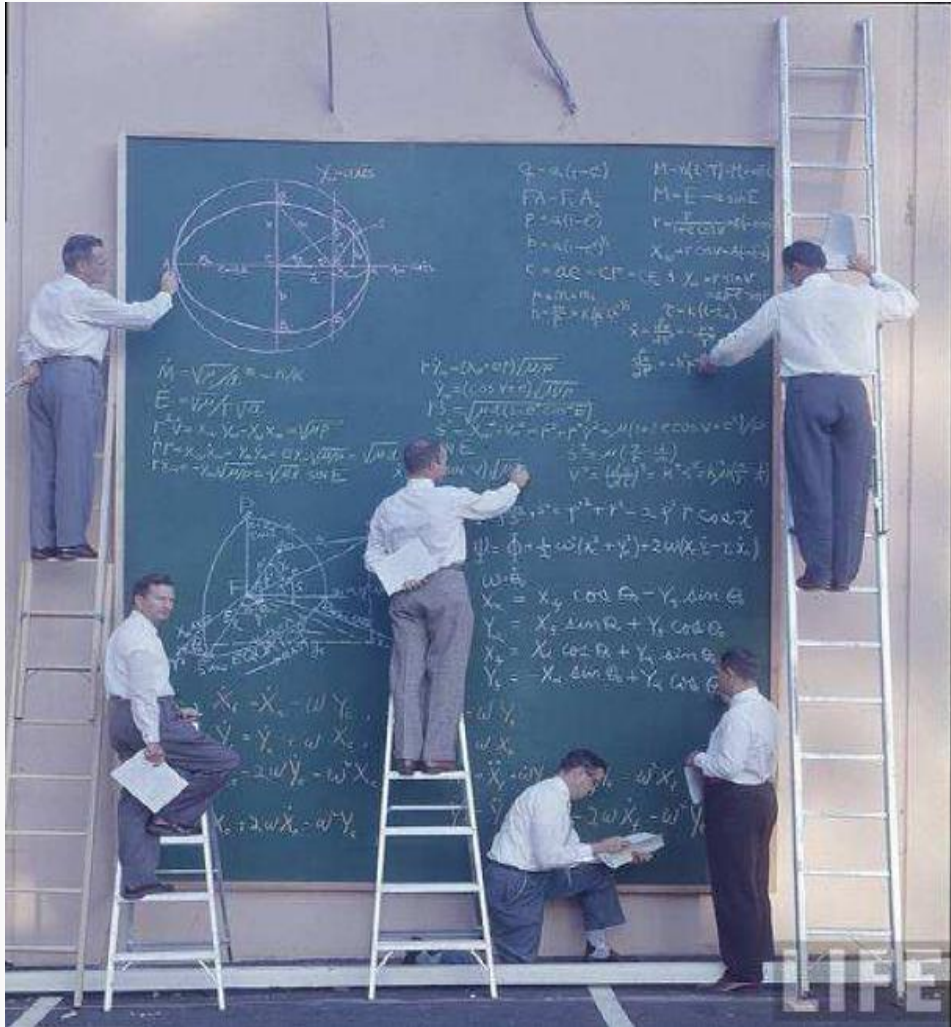
# *Mediterranean Ring*



# Conclusions

- ✓ Yet much to be done!!!!
- ✓ Hierarchical full control strategy under development
- ✓ Based on AC background, but merging with new knowledge from power electronics
- ✓ Multi-disciplinary → Much more could be presented!
- ✓ Plug-and-play
- ✓ Time scale separation

# WINPOWER philosophy: Team work



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